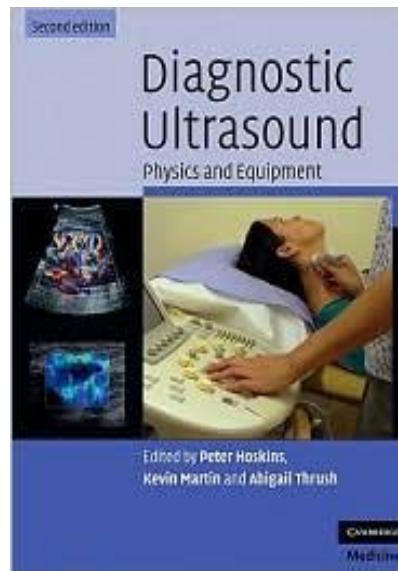




ULTRASOUND IMAGING

Recommended Textbook

- *Diagnostic Ultrasound: Physics and Equipment*, 2nd ed., by Peter R. Hoskins (Editor), Kevin Martin (Editor), Abigail Thrush (Editor) Cambridge University Press, 2010.



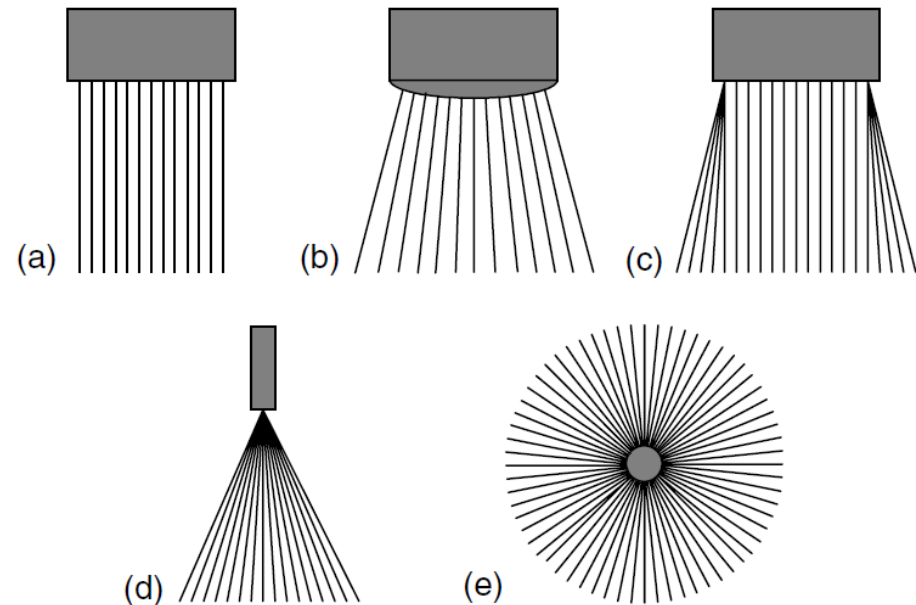
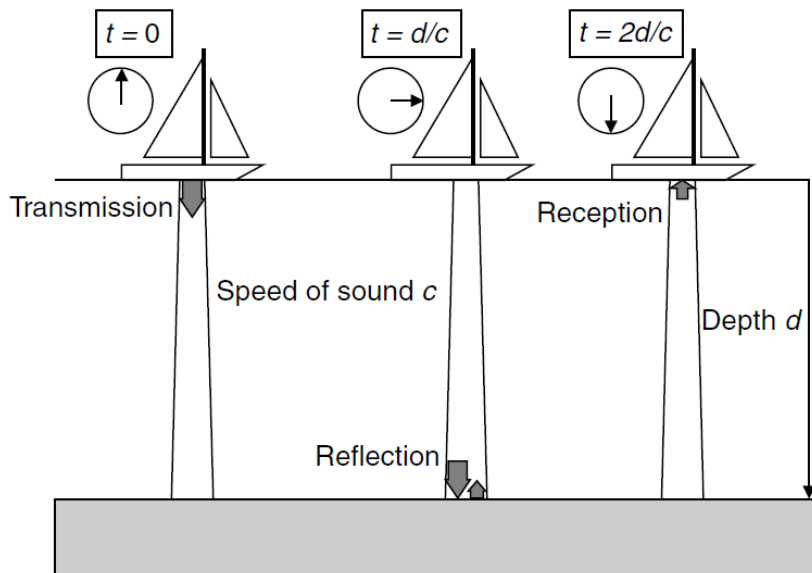
Introduction to B-mode imaging

- B-mode image is an anatomic cross-sectional image
- Constructed from echoes (reflection and scattering) of waves
- Echo is displayed at a point in image, which corresponds to relative position of its origin within the body cross section
- Brightness of image at each point is related to strength of echo
 - ▣ Term B-mode stands for Brightness-mode



Echo Ranging

- To display each echo in a position corresponding to that of the interface or feature (known as a target) that caused it, the B-mode system needs two pieces of information:
 - ▣ (1) Range (distance) of the target from the transducer
 - ▣ (2) Position and orientation of the ultrasound beam



Ultrasound Physics

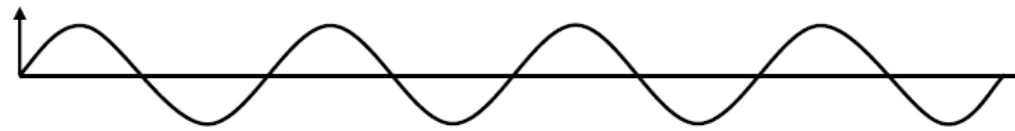
- Sound waves used to form medical images are longitudinal waves, which propagate (travel) only through a physical medium (usually tissue or liquid)
 - ▣ Characterized by frequency, wavelength, speed and phase

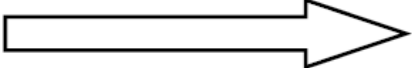
$$c = f\lambda$$

$$\text{Speed of sound } c = \sqrt{\frac{k}{\rho}}$$

Material	c (m s ⁻¹)
Liver	1578
Kidney	1560
Amniotic fluid	1534
Fat	1430
Average tissue	1540
Water	1480
Bone	3190–3406
Air	333

Pressure



Direction of propagation 



Particle displacement

Ultrasound Physics

- Medical ultrasound frequencies used in the range 2–15 MHz
 - Higher frequencies are now utilized for special applications
 - Resolution proportional to wavelength

f (MHz)	λ (mm)
2	0.77
5	0.31
10	0.15
15	0.1

- Acoustic impedance $z = p/v$

- p is the local pressure and v is the local particle velocity.
- Analogous to electrical impedance (or resistance R)

$$z = \sqrt{\rho k} = \rho c$$

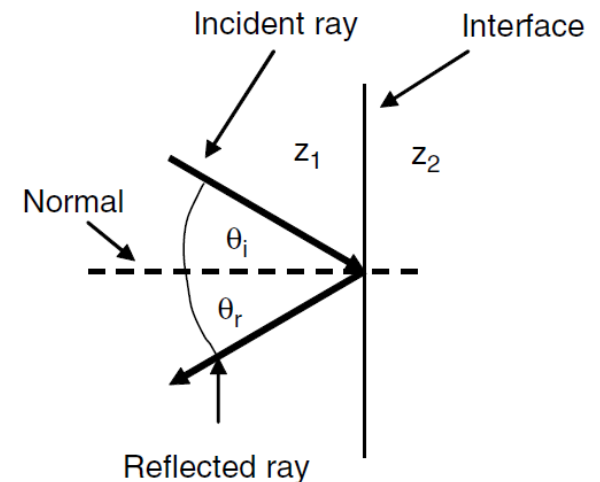
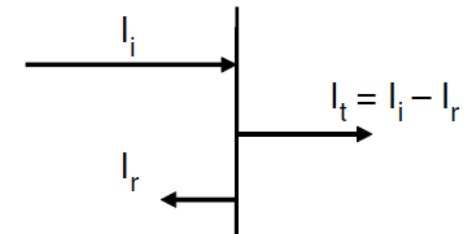
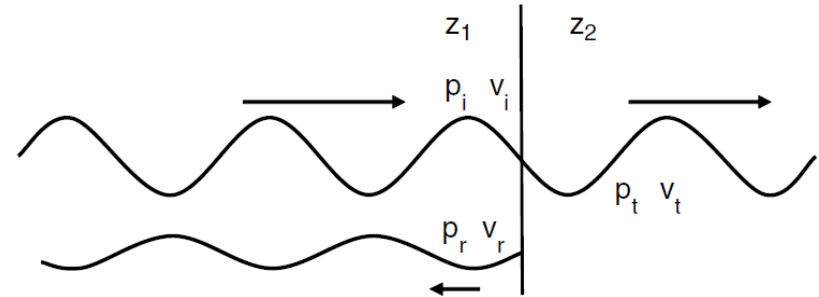
Material	z ($\text{kg m}^{-2} \text{s}^{-1}$)
Liver	1.66×10^6
Kidney	1.64×10^6
Blood	1.67×10^6
Fat	1.33×10^6
Water	1.48×10^6
Air	430
Bone	6.47×10^6

Ultrasound Physics

□ Reflection: Large Interfaces

$$R_A = \frac{P_r}{P_i} = \frac{z_2 - z_1}{z_2 + z_1}$$

$$\frac{I_r}{I_i} = R_i = R_A^2$$



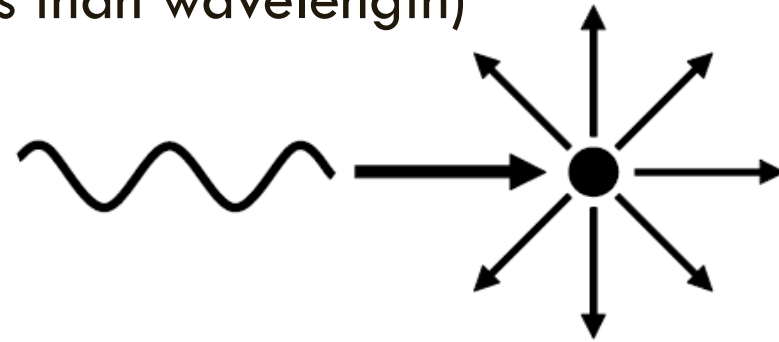
$$\theta_r = \theta_i$$

Interface	R_A
Liver-kidney	0.006
Kidney-spleen	0.003
Blood-kidney	0.009
Liver-fat	0.11
Liver-bone	0.59
Liver-air	0.9995

Ultrasound Physics

- Scattering: **Small Interfaces** (size less than wavelength)

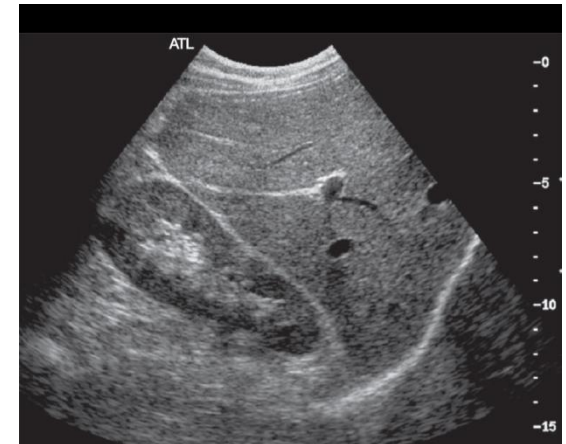
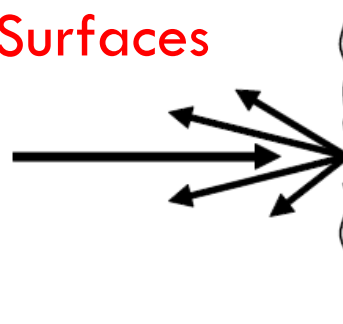
$$W_s \propto \frac{d^6}{\lambda^4} \propto d^6 f^4$$



- Two important aspects of scattering:

- ▣ Ultrasonic power scattered back is small compared to reflections
- ▣ Beam angle-independent appearance in the image unlike reflections

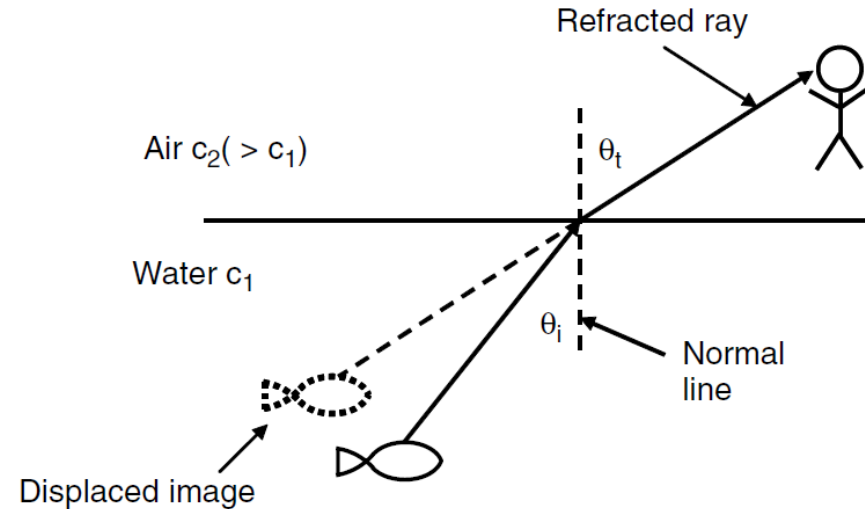
- Diffuse Reflection: **Rough Surfaces**



Ultrasound Physics

□ Refraction: Snell's law

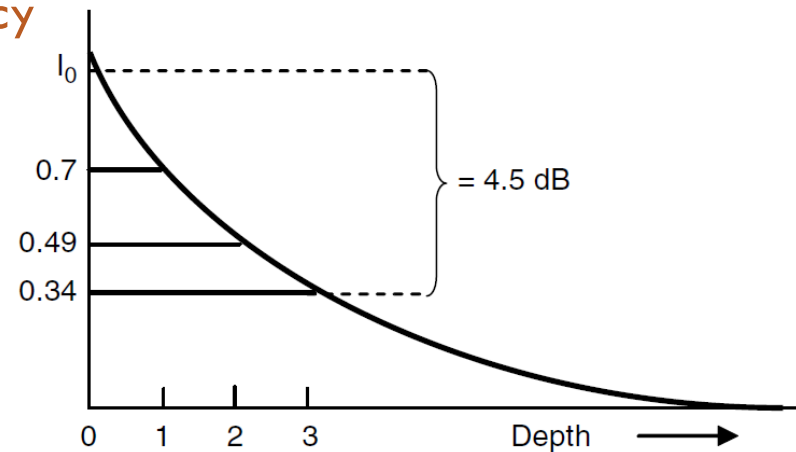
$$\frac{\sin \theta_i}{\sin \theta_t} = \frac{c_1}{c_2}$$



□ Attenuation: gradual loss of beam energy

▣ Depends on both distance and frequency

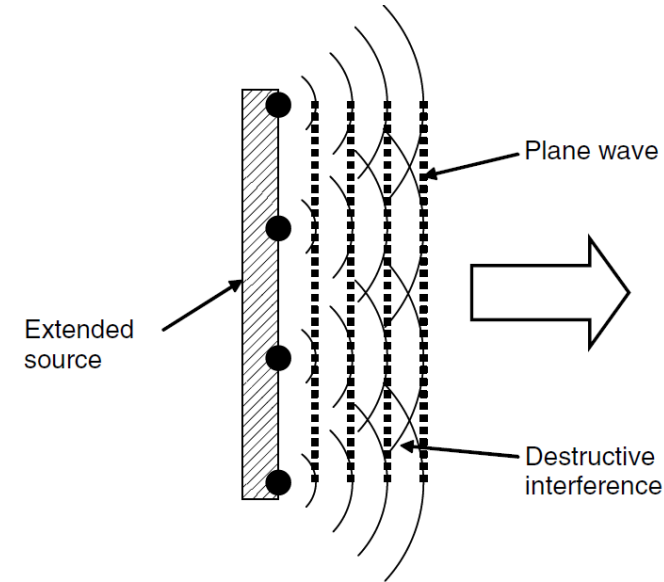
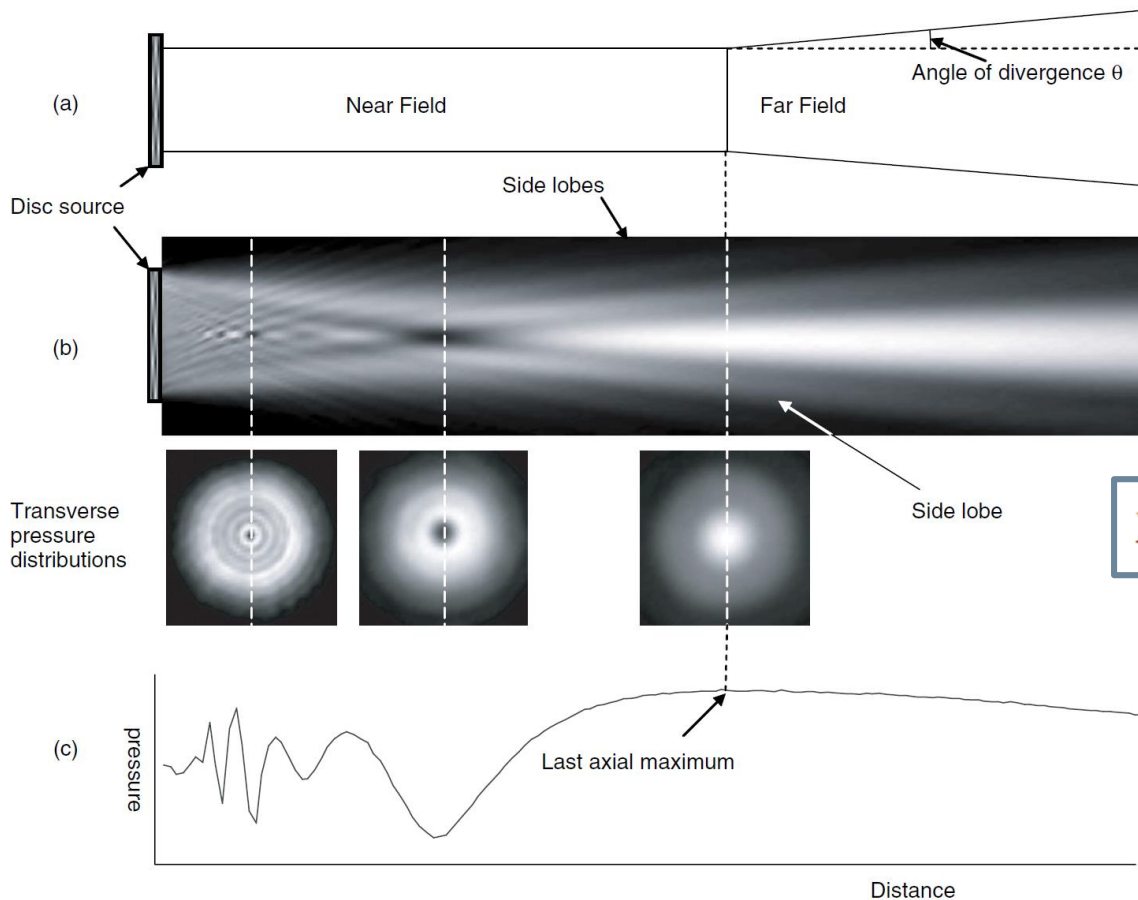
Tissue	Attenuation (dB cm ⁻¹ MHz ⁻¹)
Liver	0.399
Brain	0.435
Muscle	0.57
Blood	0.15
Water	0.02
Bone	22



Ultrasound Physics

□ Interference and diffraction

▣ Constructive/Destructive interference

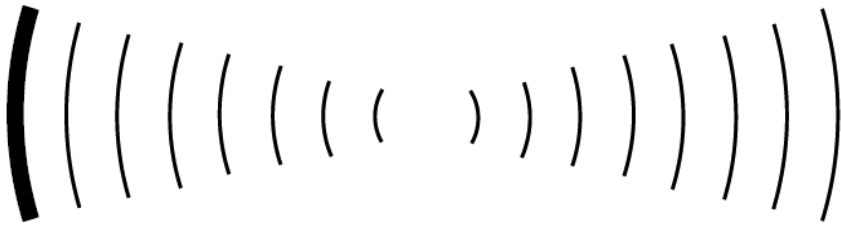


$$\text{near field length} = a^2/\lambda$$

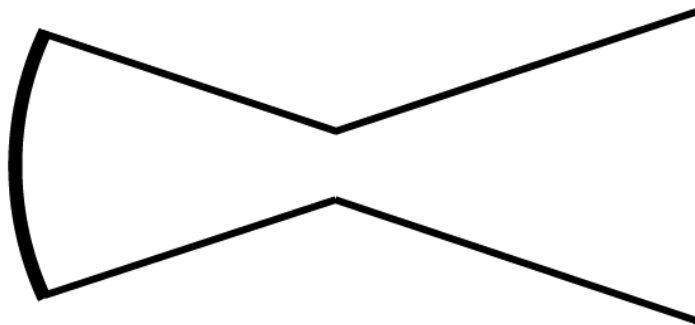
$$\sin \theta = 0.61 (\lambda/a)$$

Ultrasound Physics

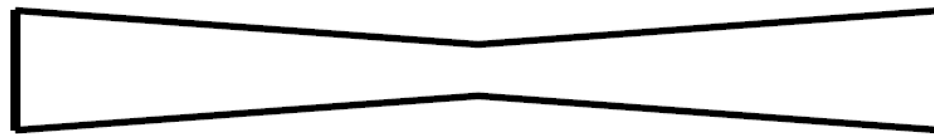
□ Focusing: narrower ultrasound beam



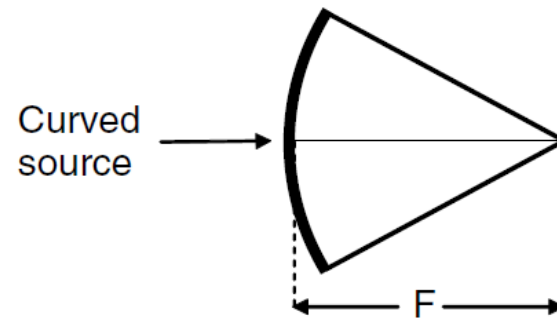
(a)



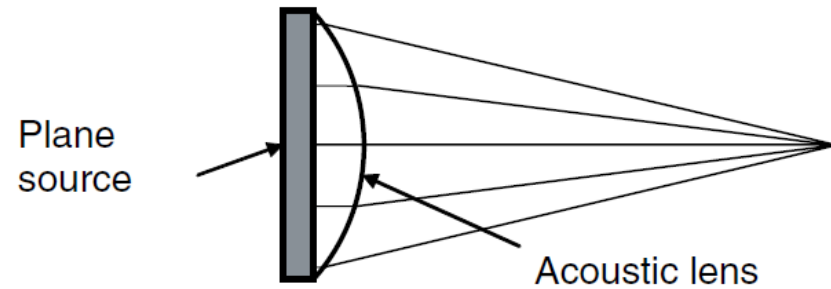
(b)



(c)



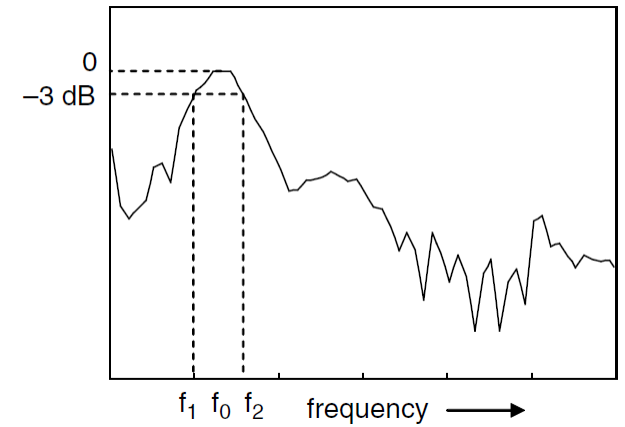
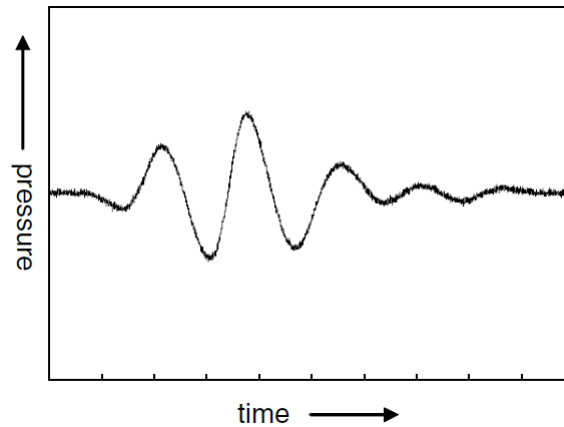
(a)



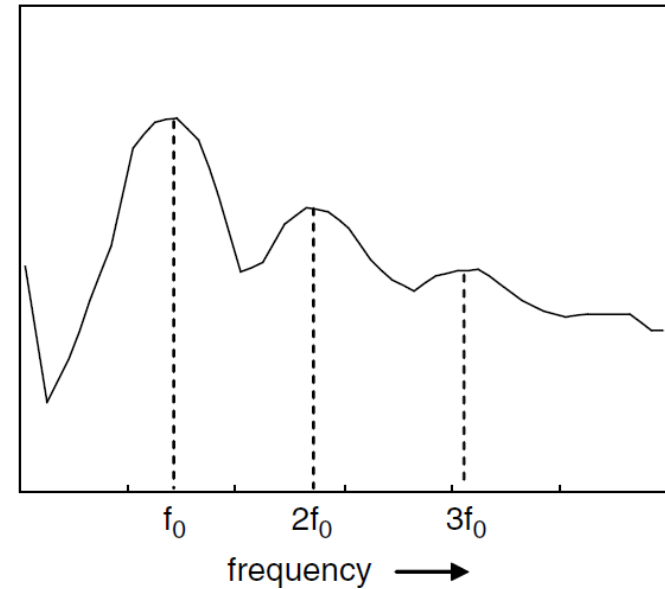
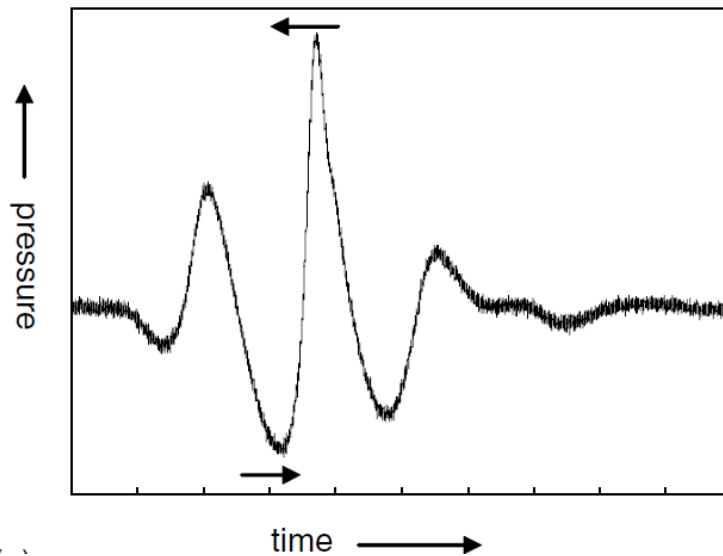
(b)

Ultrasound Physics

□ Ultrasound pulse

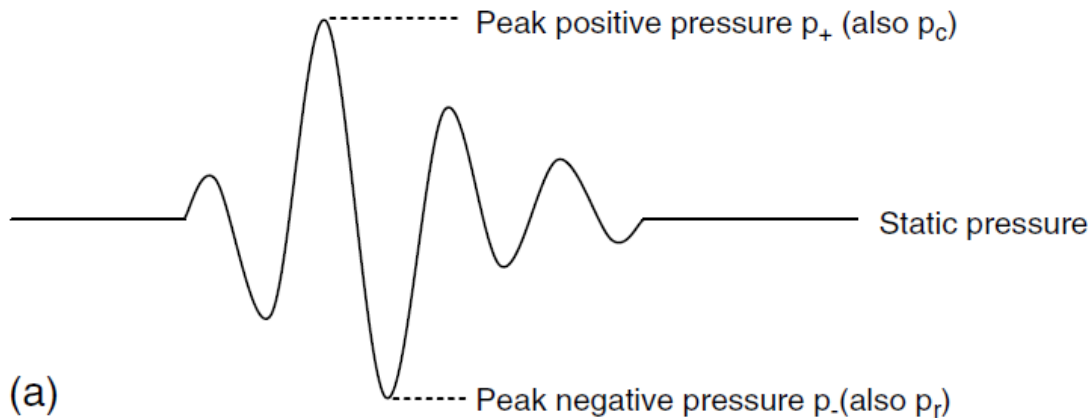


□ Harmonic Imaging

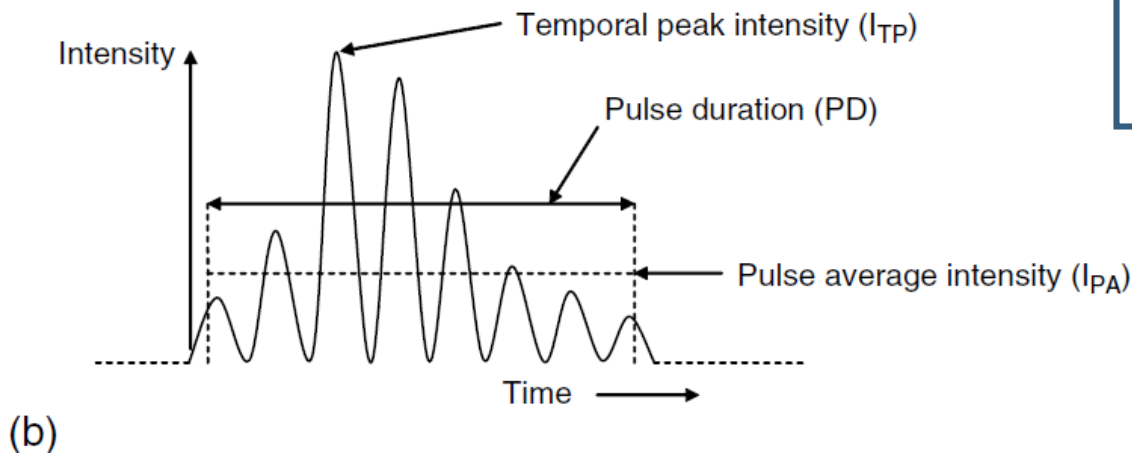


Ultrasound Physics

□ Acoustic pressure and intensities within ultrasound beam



$$I = \frac{p^2}{z}$$

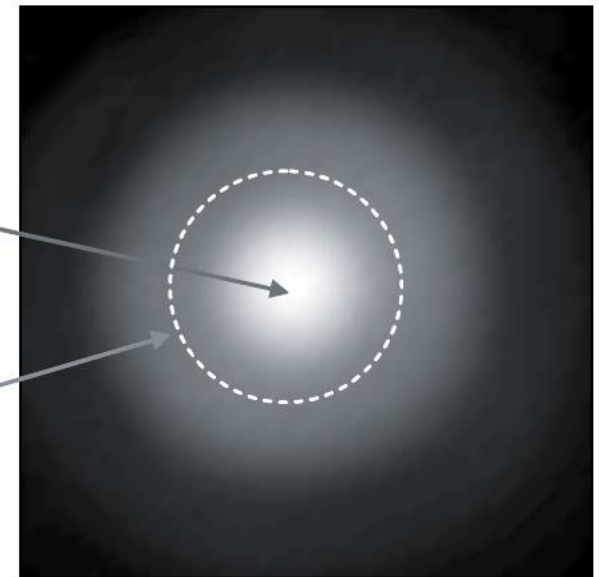
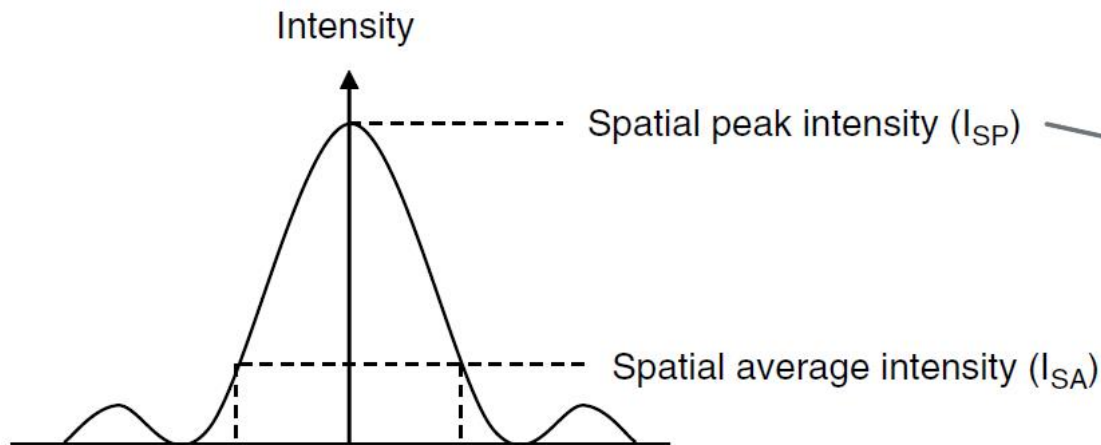
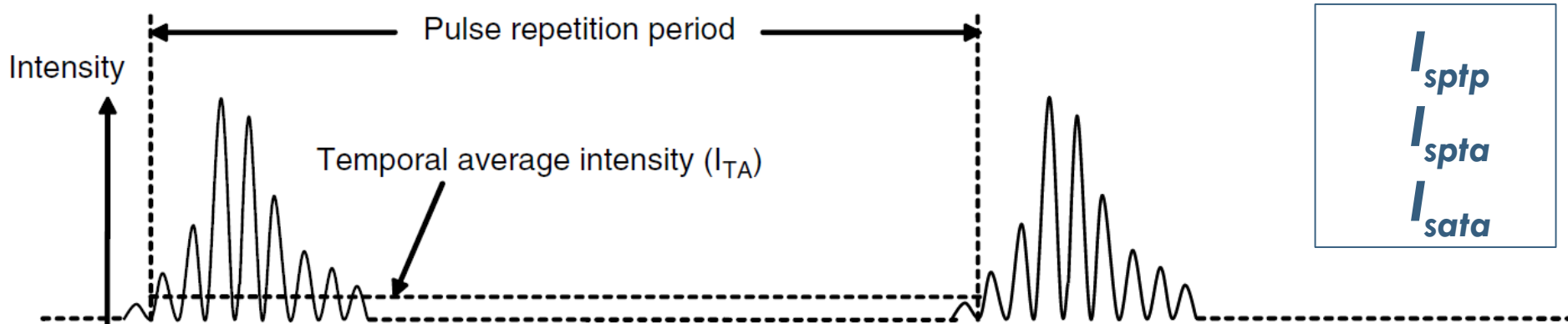


$$PD = 1.25 \times (T_{90} - T_{10})$$

$$I_{PA} = PII / PD$$

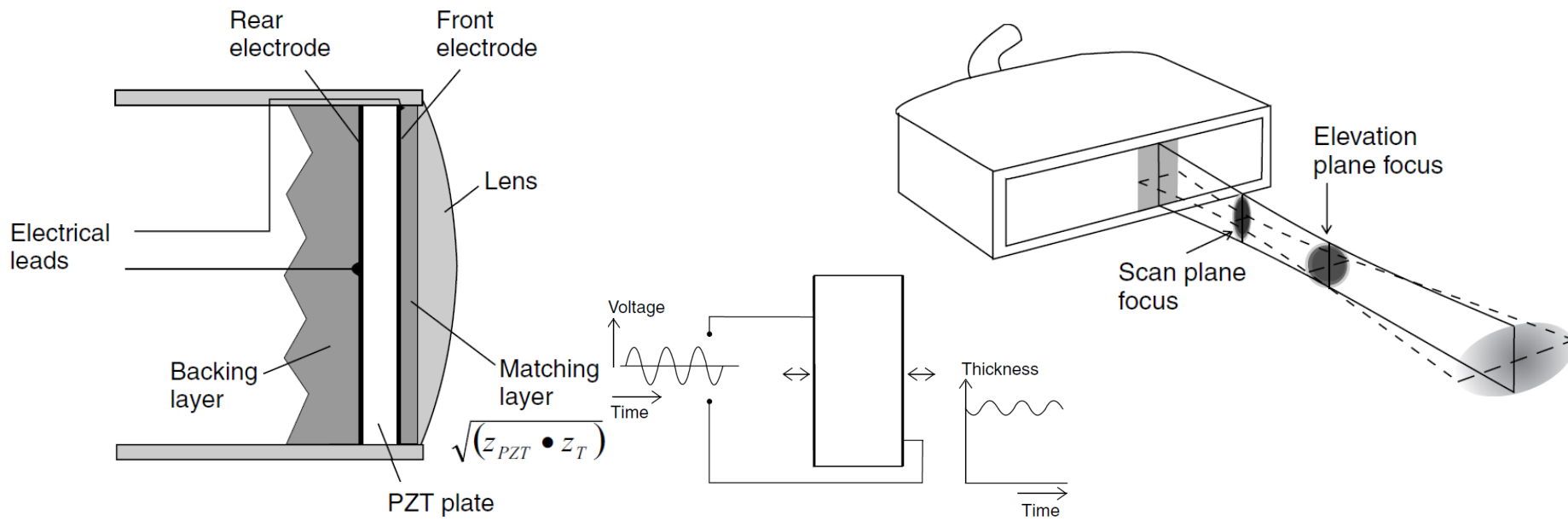
Ultrasound Physics

□ Acoustic pressure and intensities within ultrasound beam



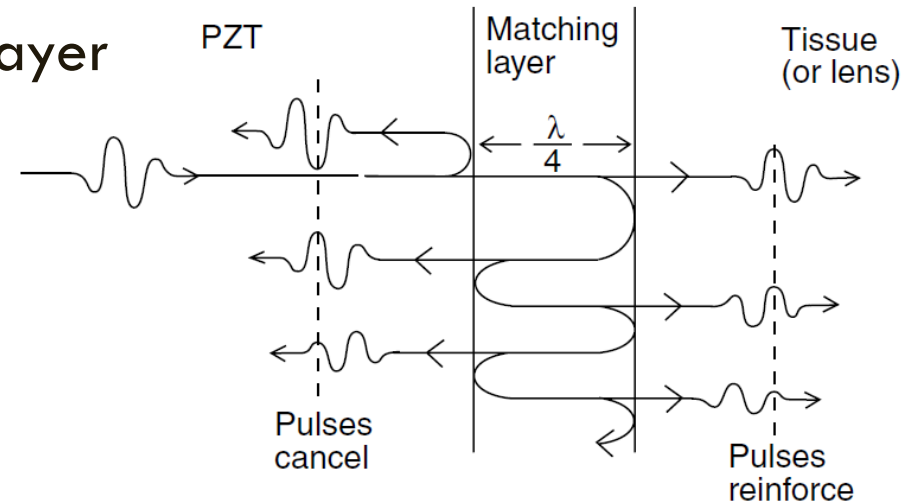
Transducers and Beamforming

- Transducer: device that actually converts electrical transmission pulses into ultrasonic pulses and, conversely, ultrasonic echo pulses into electrical echo signals
- Beamformer: part of scanner that determines the shape, size and position of the interrogating beams by controlling electrical signals to and from the transducer array elements

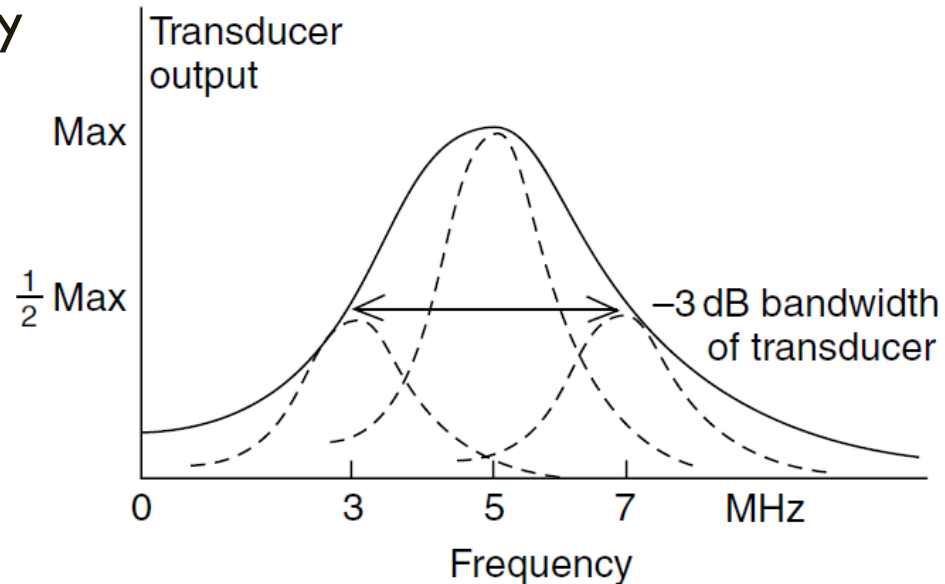


Transducers and Beamforming

□ Quarter-wavelength matching layer

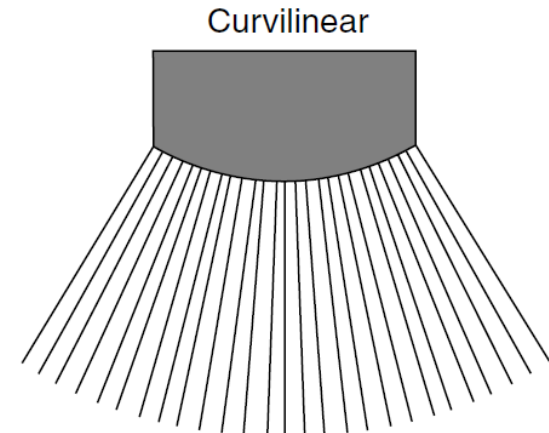
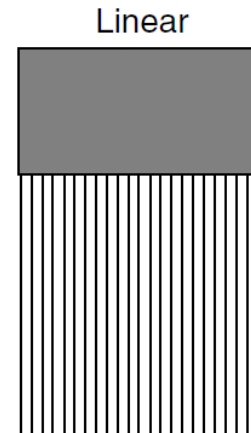
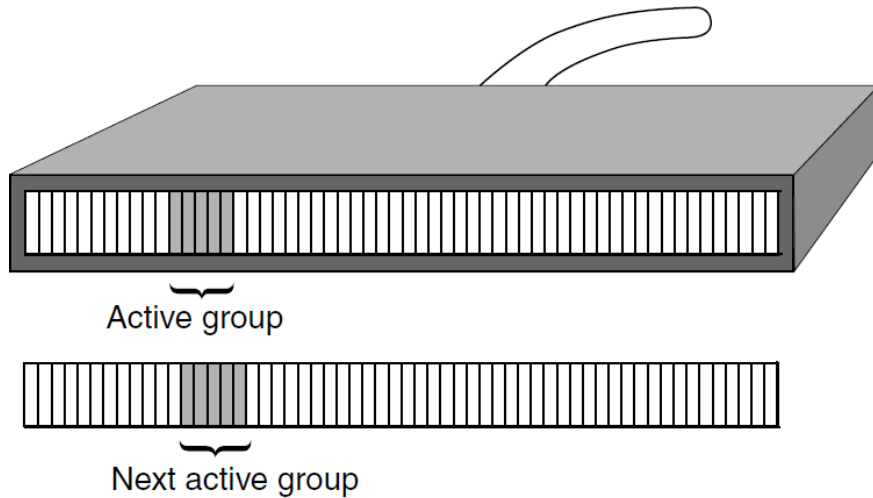
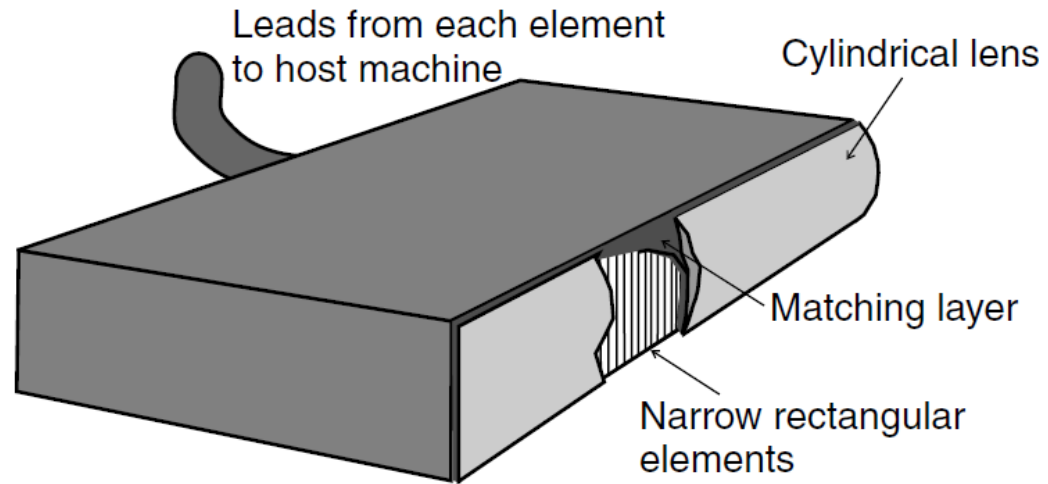
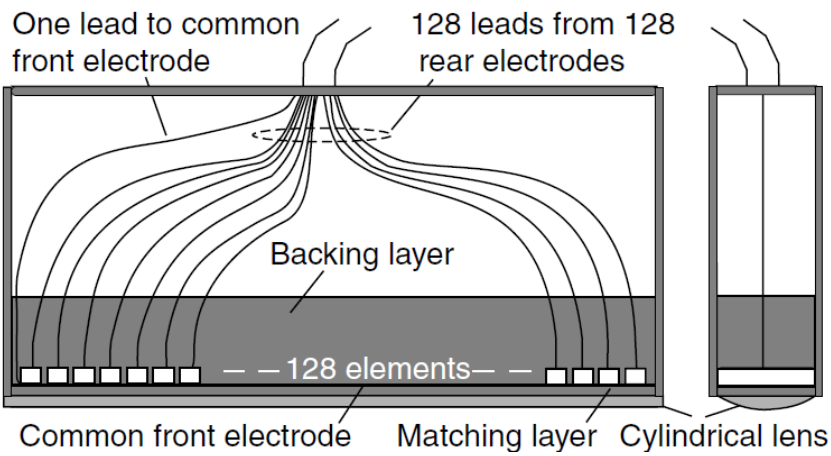


□ Bandwidth for multi-frequency transducers



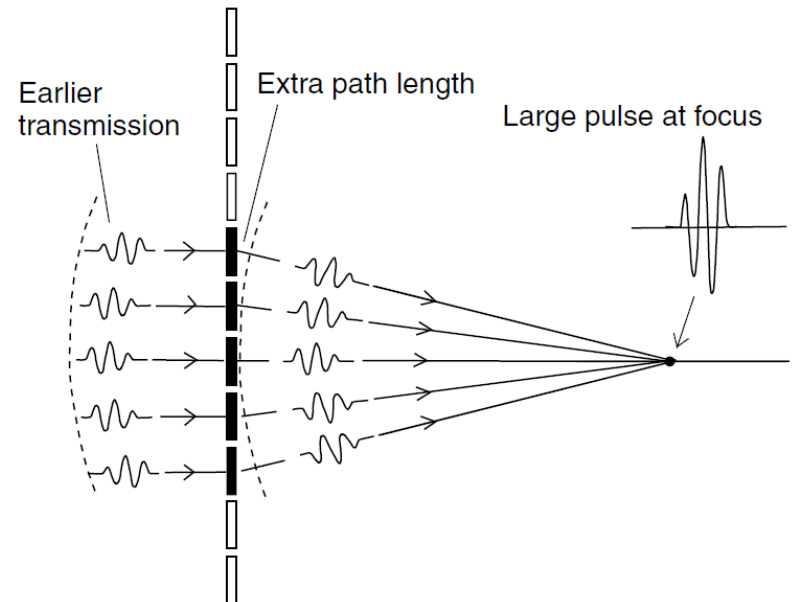
Transducers and Beamforming

Linear- and curvilinear-array transducers



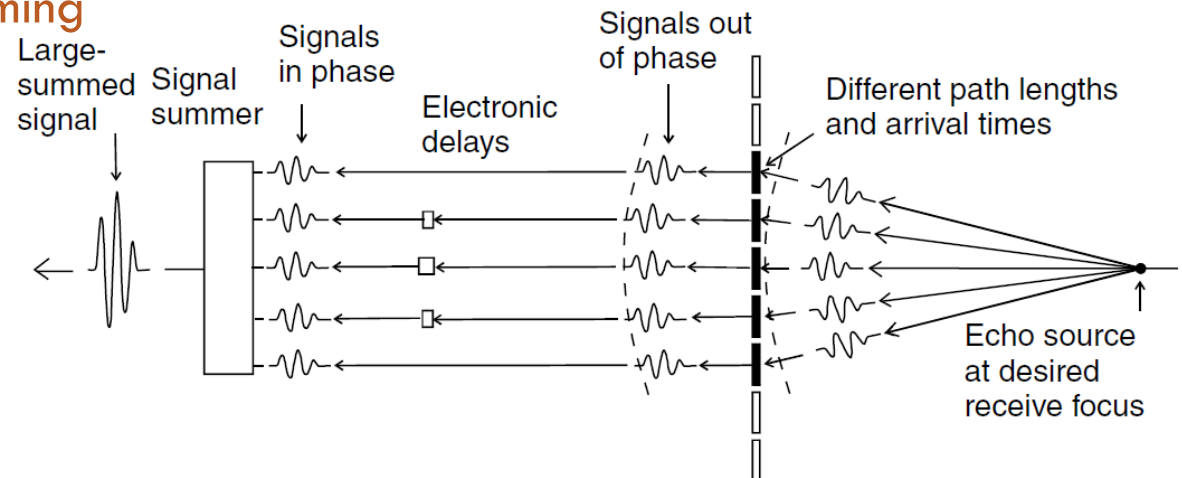
Transducers and Beamforming

□ Transmission Focusing



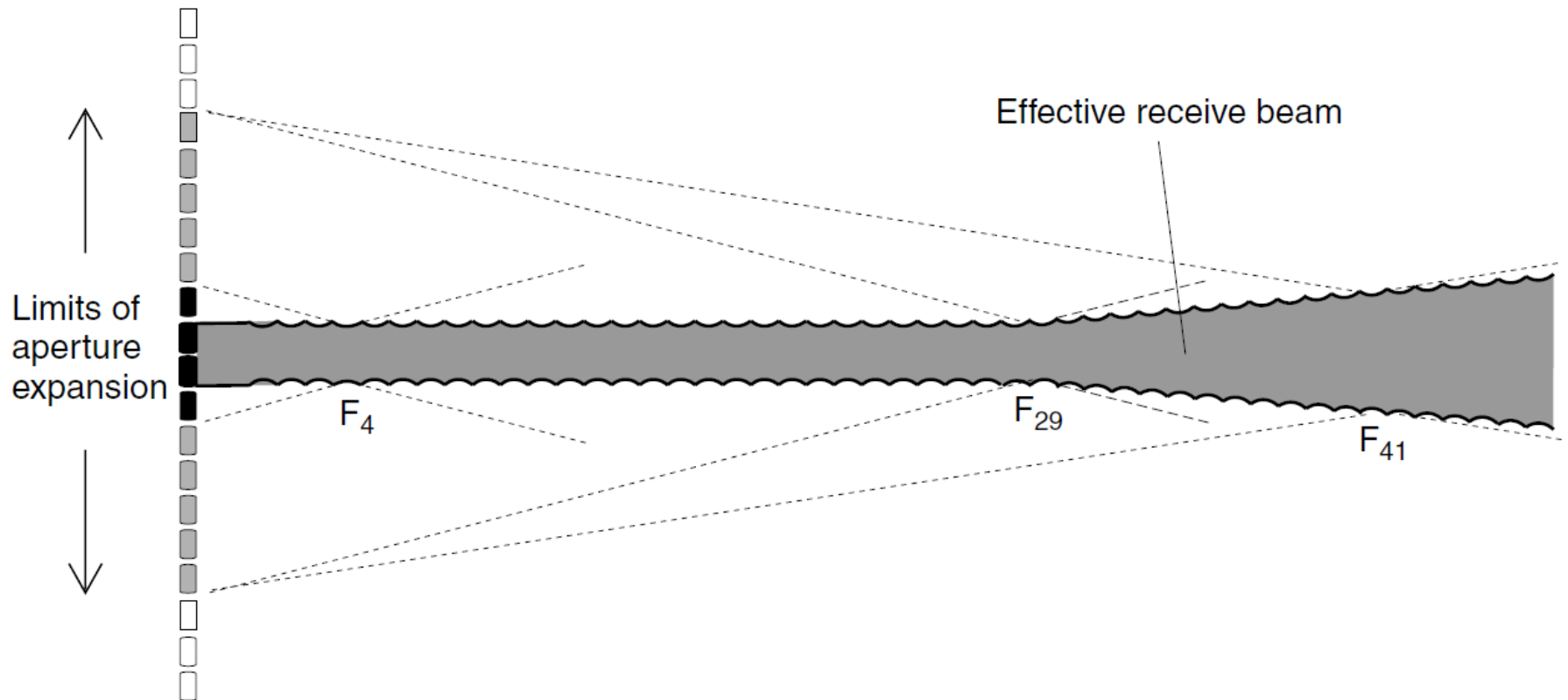
□ Reception focusing

▣ Delay-Sum beamforming



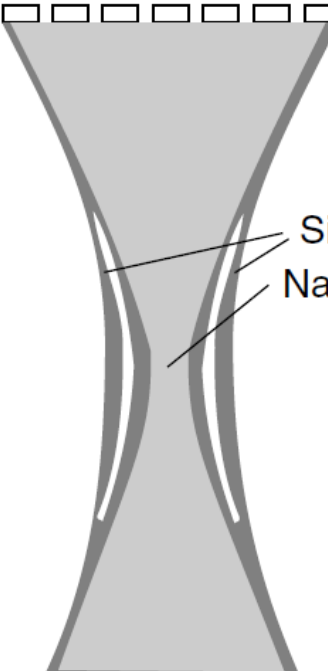
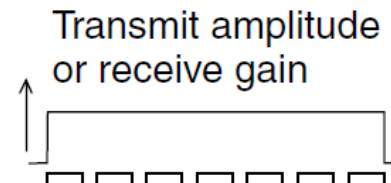
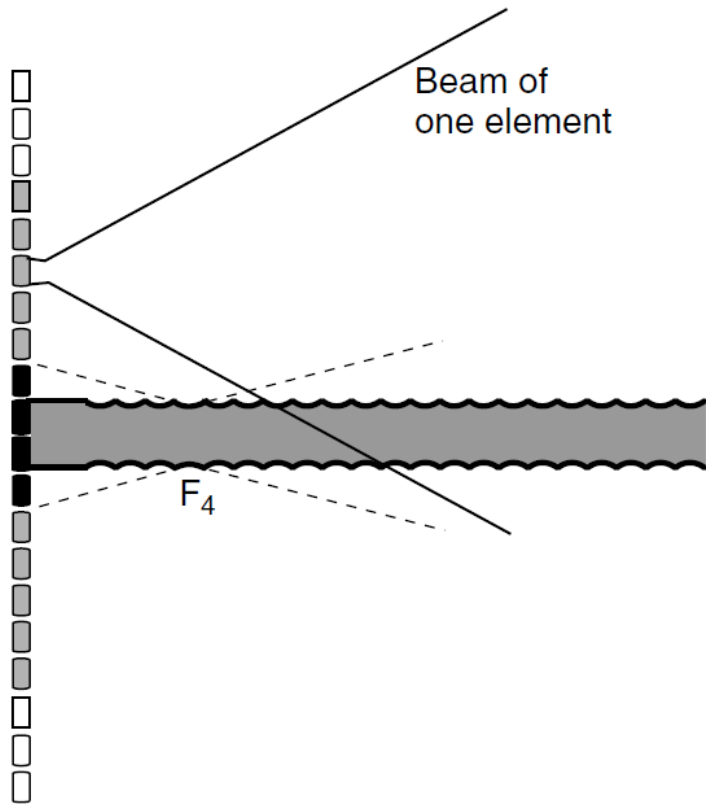
Transducers and Beamforming

□ Dynamic reception focusing

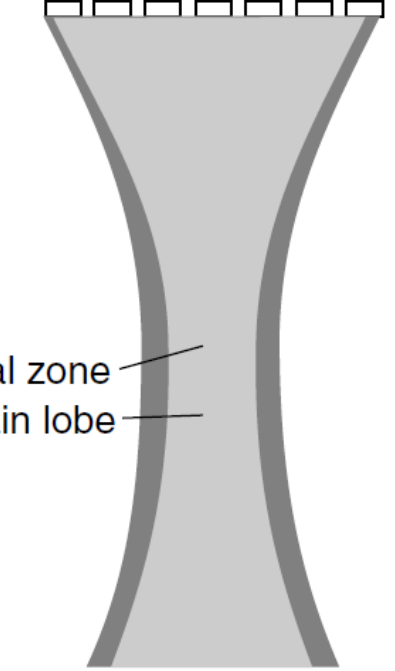
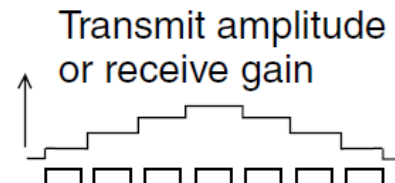


Transducers and Beamforming

- Beamforming: selecting active elements and apodization



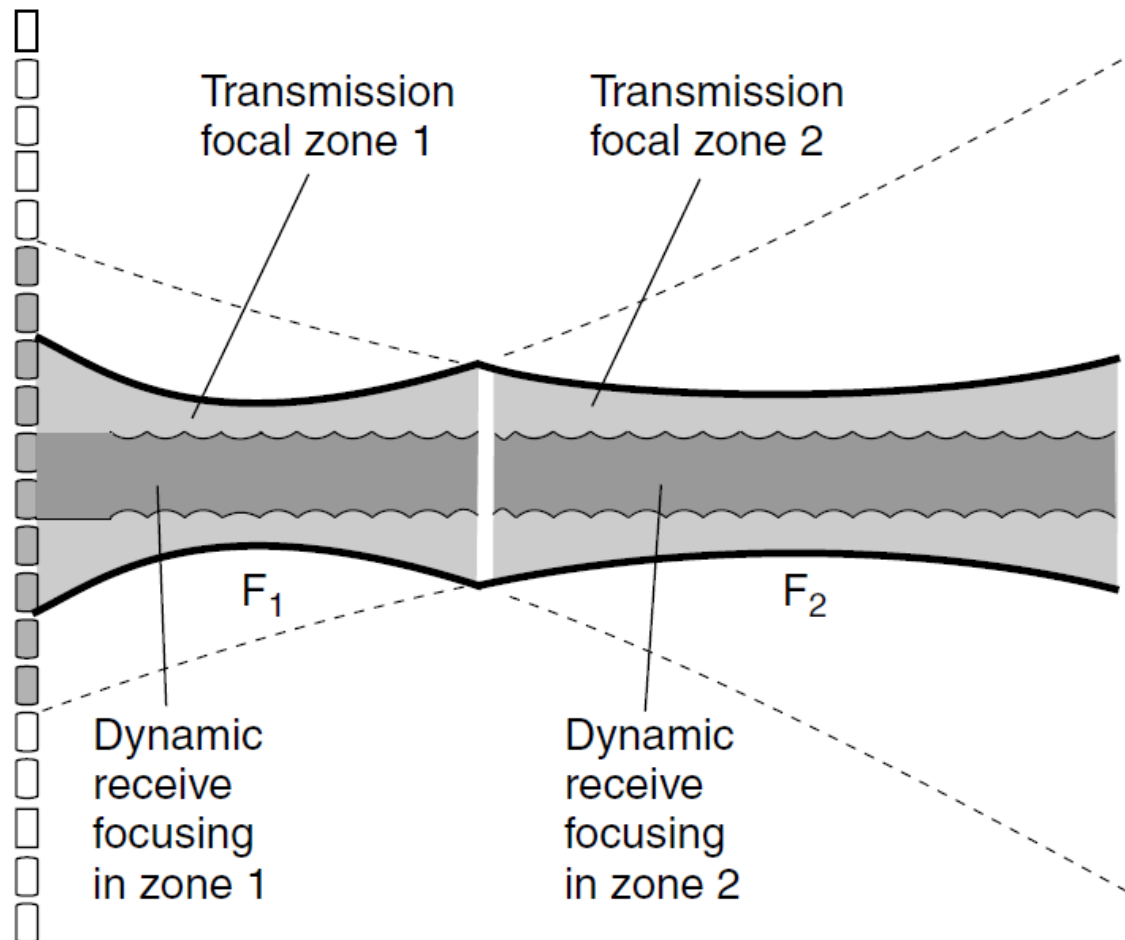
Uniform excitation



Non-uniform excitation (apodization)

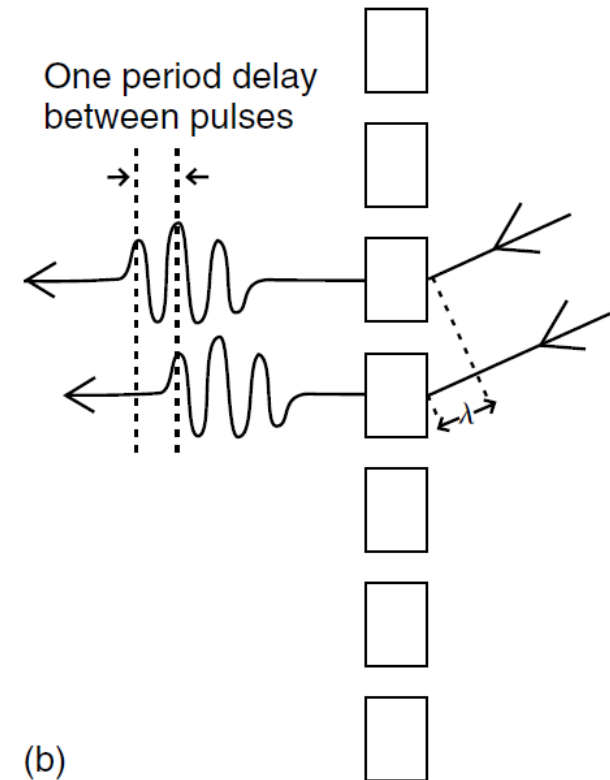
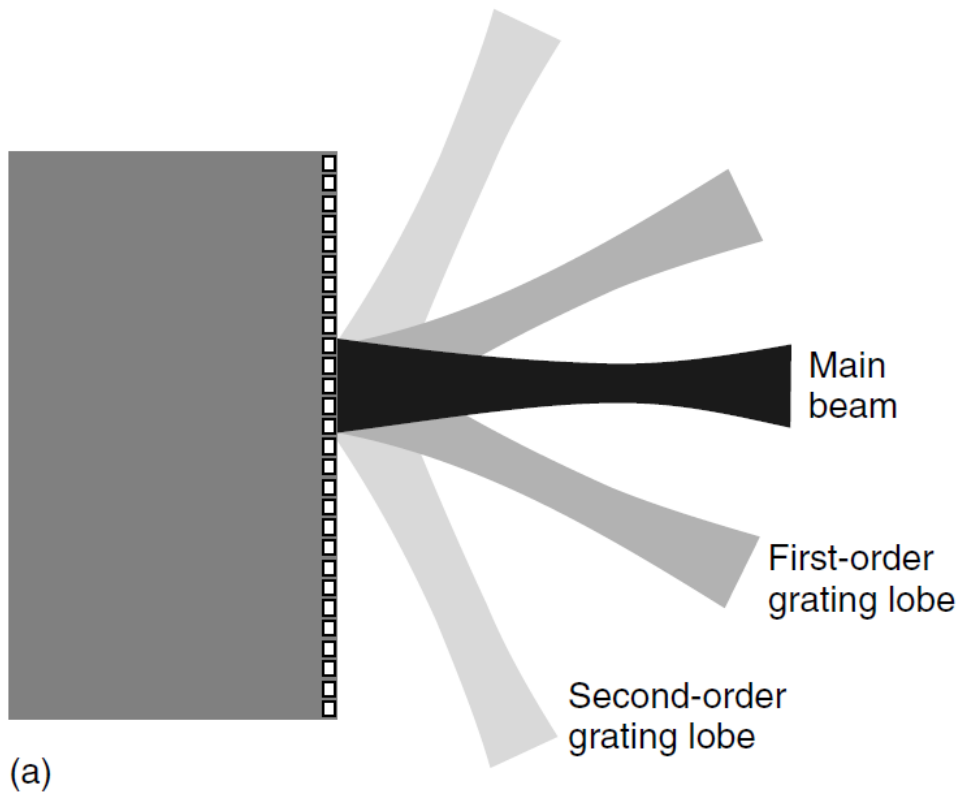
Transducers and Beamforming

- Beamforming: Multiple Transmission zones



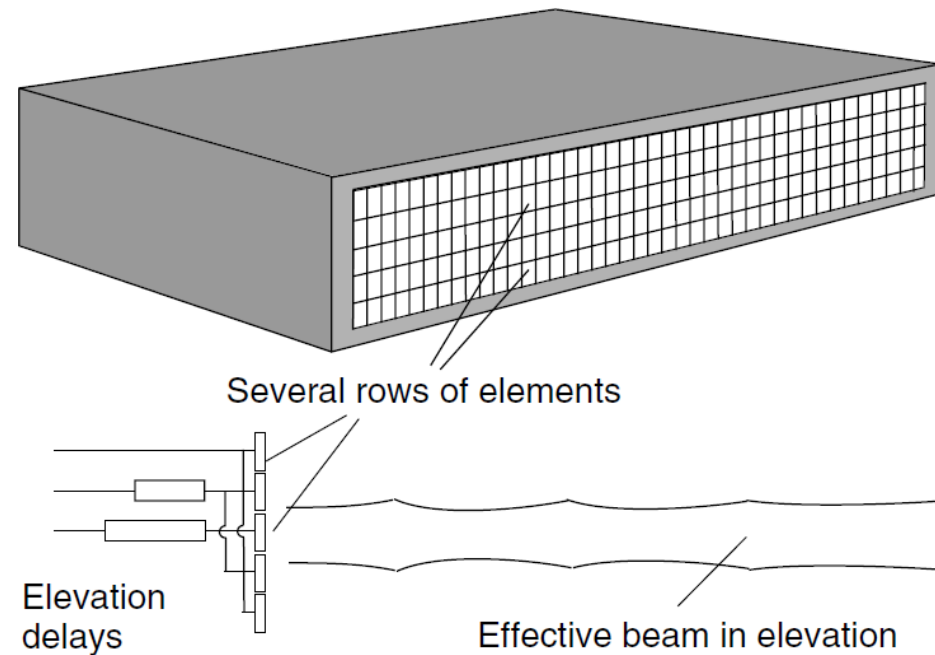
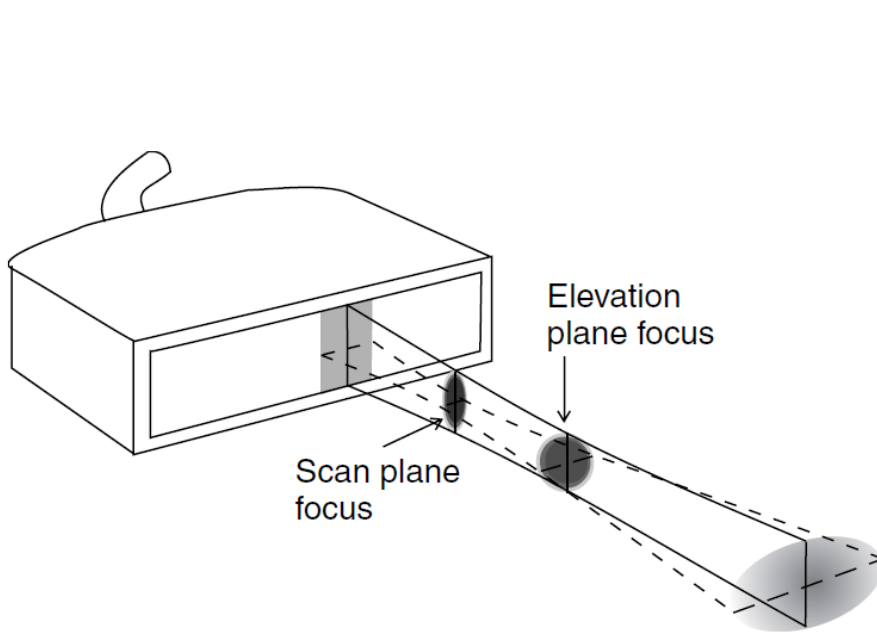
Transducers and Beamforming

- Beamforming: Grating lobes
 - ▣ No grating lobes, if the center-to-center distance between elements is half a wavelength or less



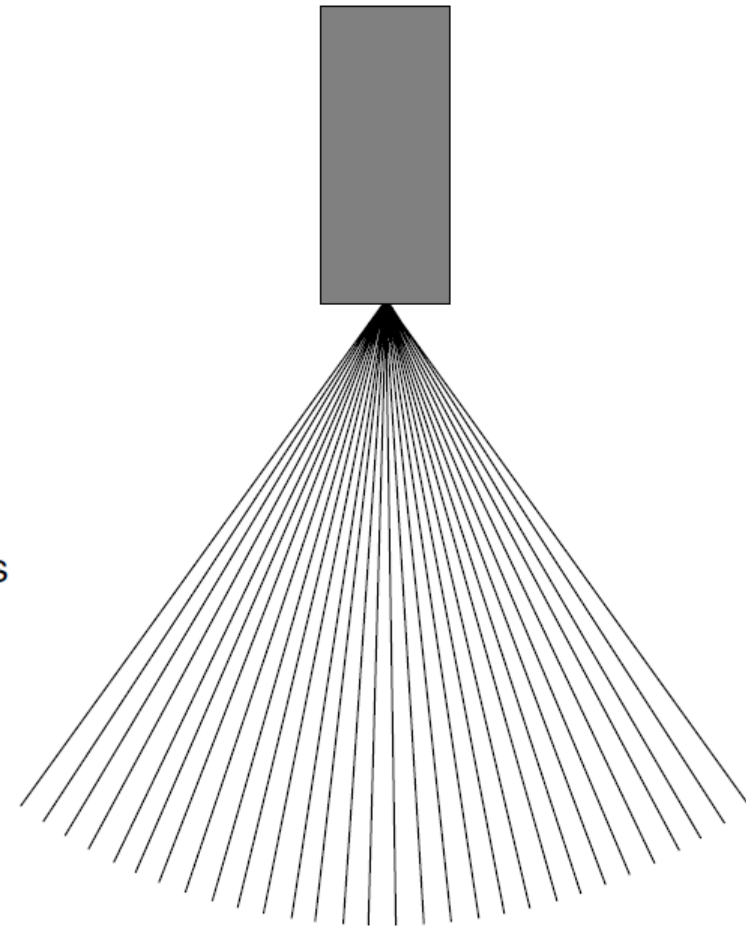
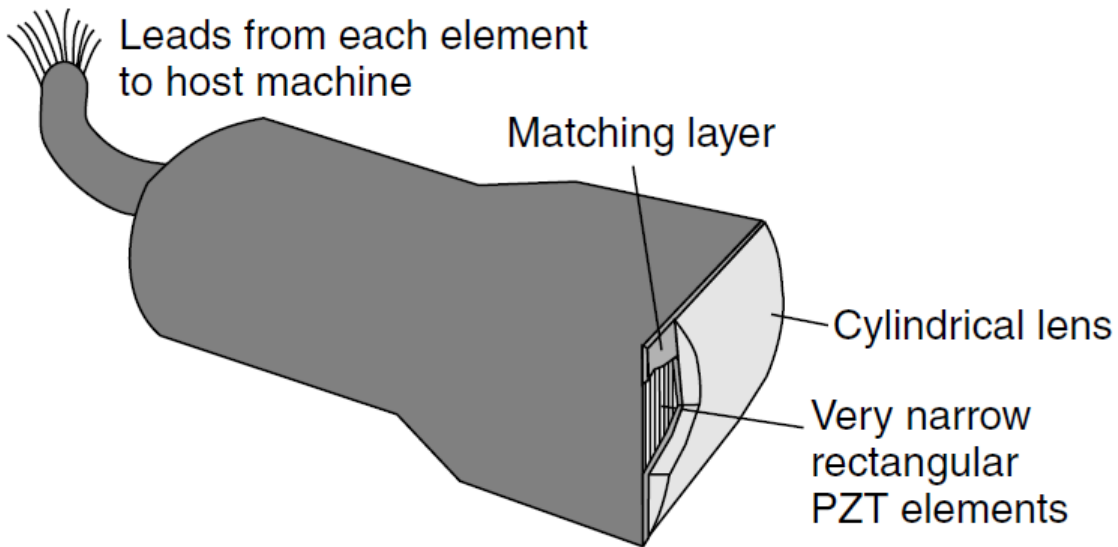
Transducers and Beamforming

- Slice thickness: elevation direction
 - ▣ 1.5D or 2D arrays



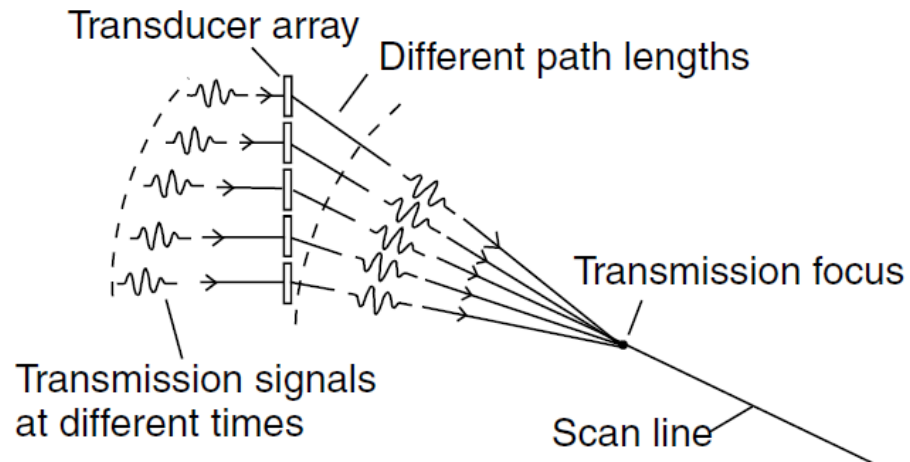
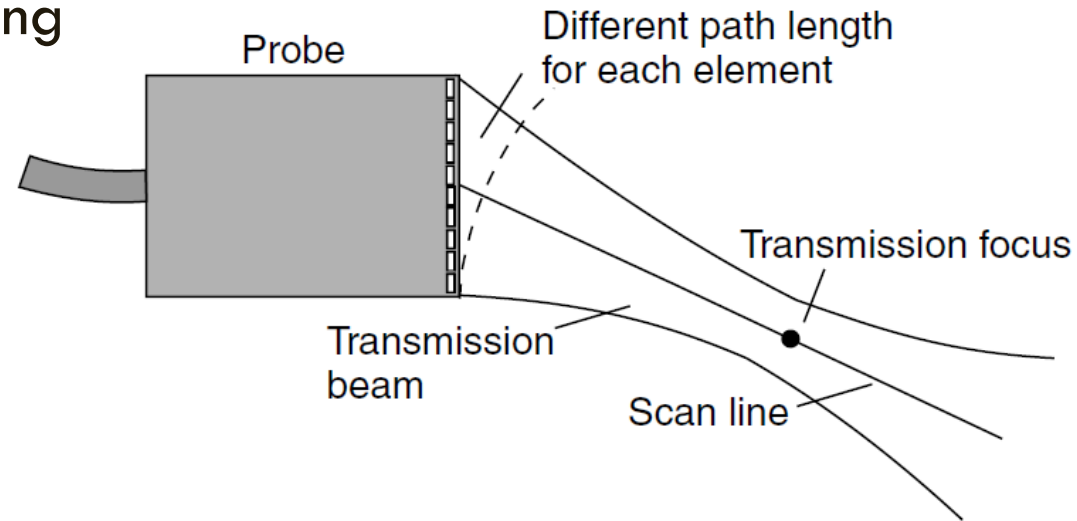
Transducers and Beamforming

□ Phased Array transducers



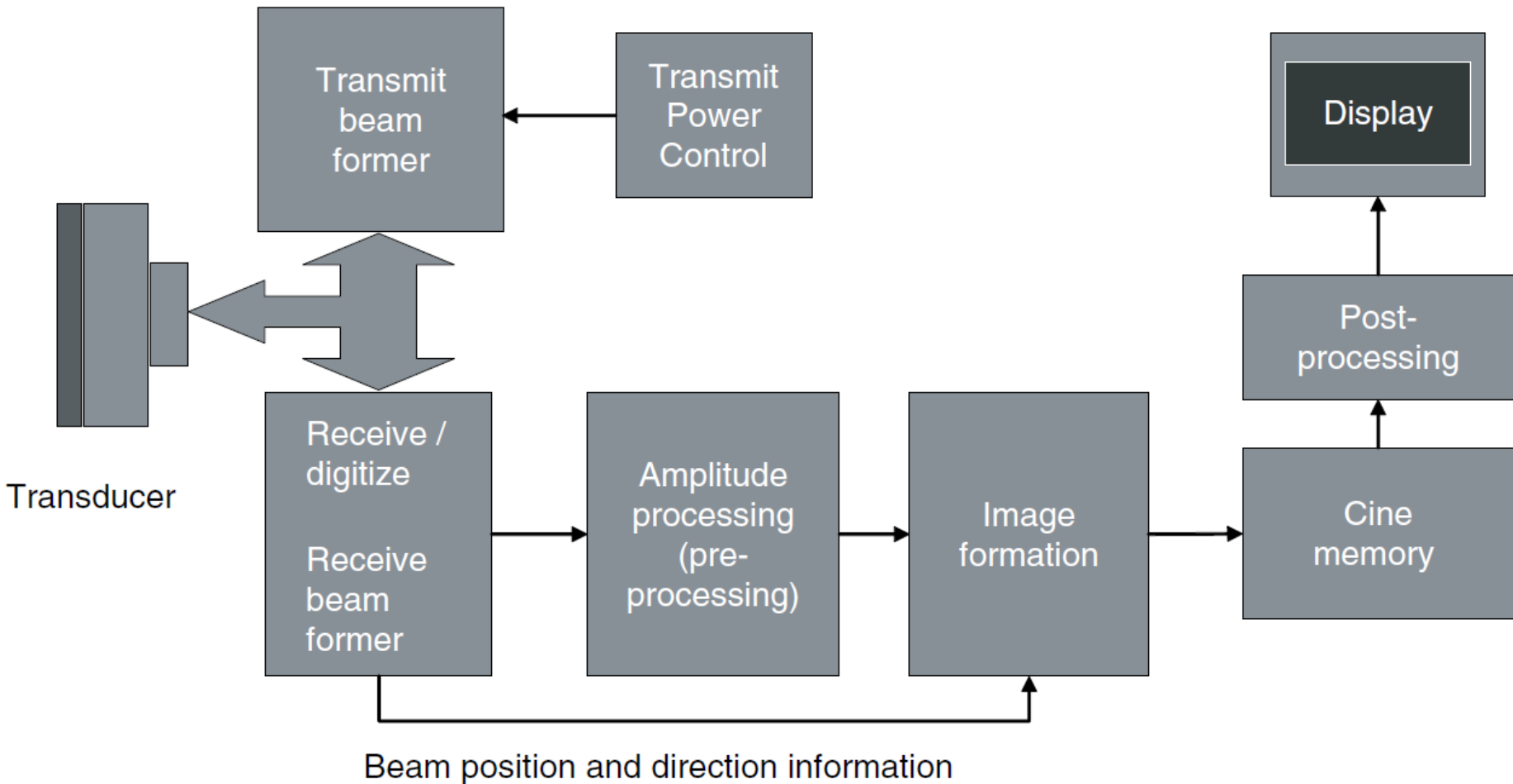
Transducers and Beamforming

□ Electronic steering/focusing



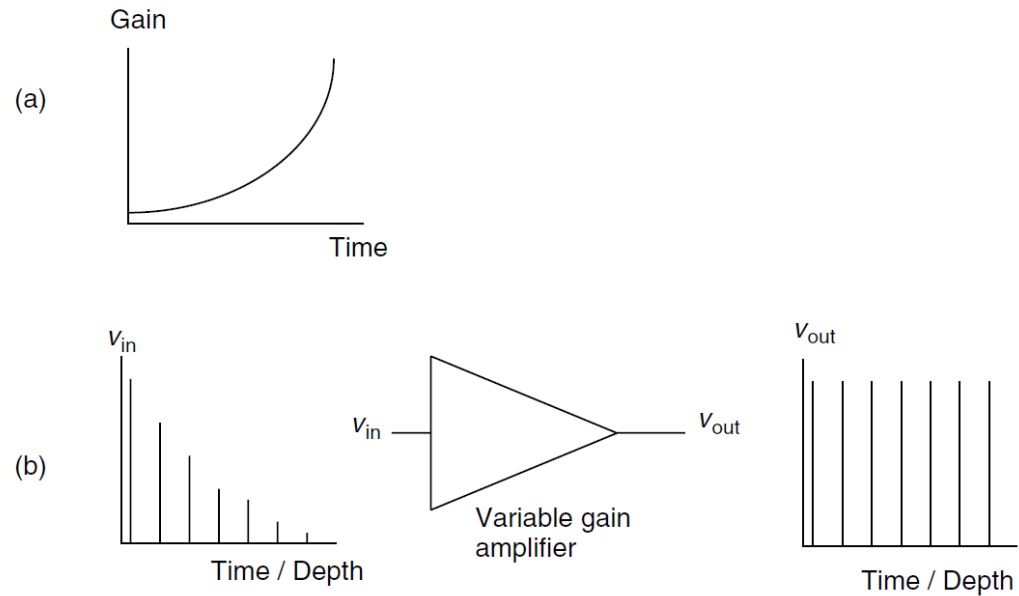
B-Mode Instrumentation

Processing block diagram



B-Mode Instrumentation

□ Time-Gain Compensation



TGC slide controls

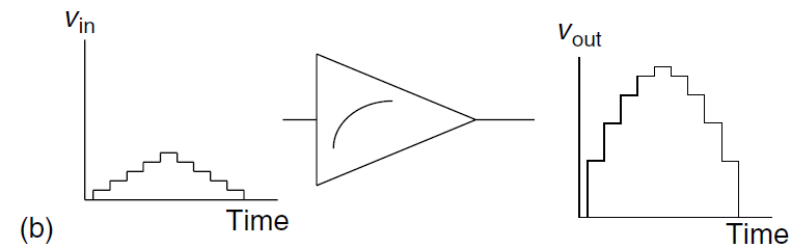
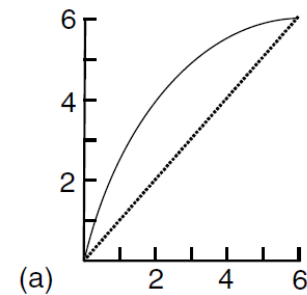
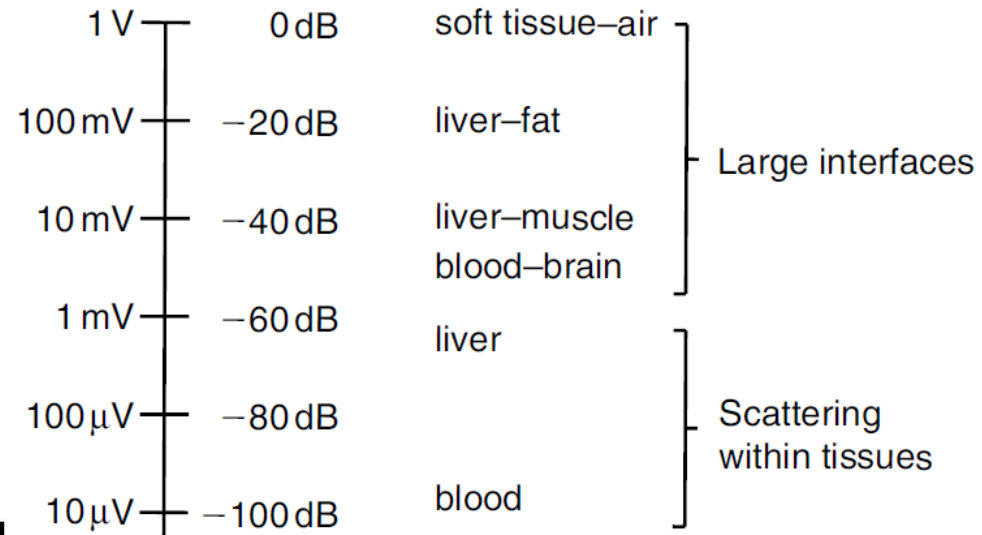
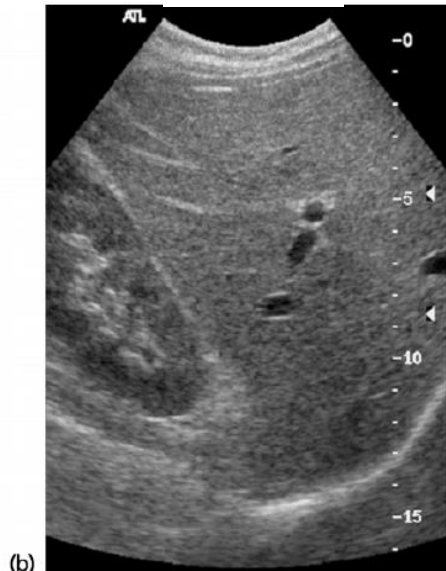
B-Mode Instrumentation

Dynamic range of echoes

Bits	Max count	DR (dB)
4	15	24
8	255	48
10	1023	60
12	4095	72

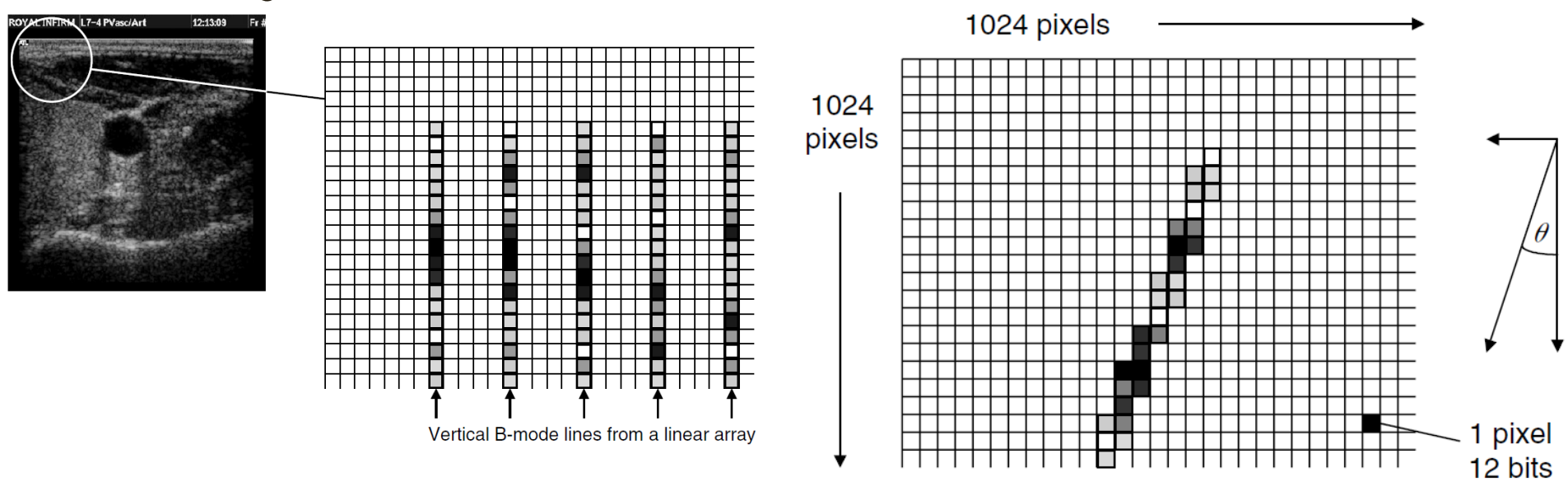
40 dB

80 dB



B-Mode Instrumentation

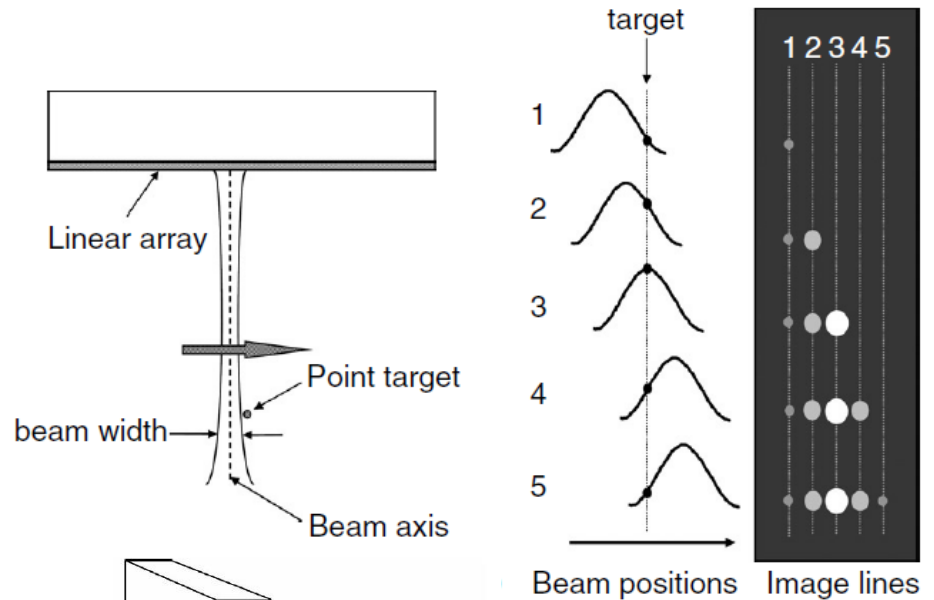
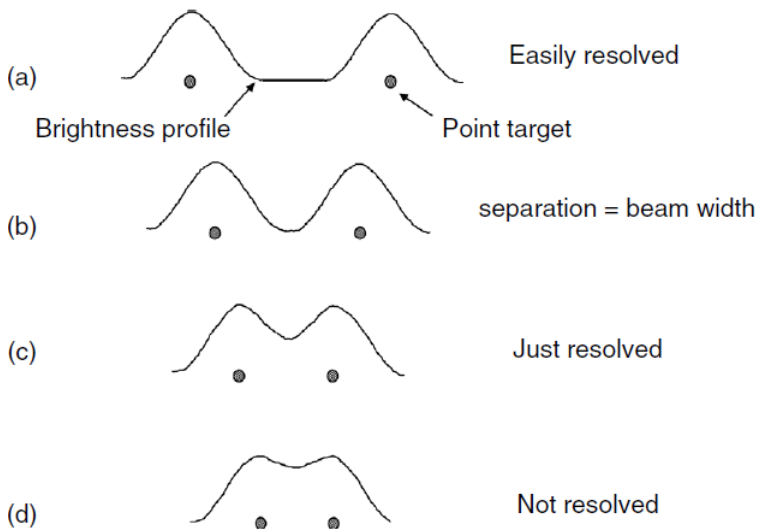
- Image reconstruction: scan conversion and interpolation



- Real-time display: frame every $1/25$ s
- Freeze: updating frame stops
- Cine Loop: recording of real-time scan as a movie
- Frame Averaging: moving average filter to improve SNR

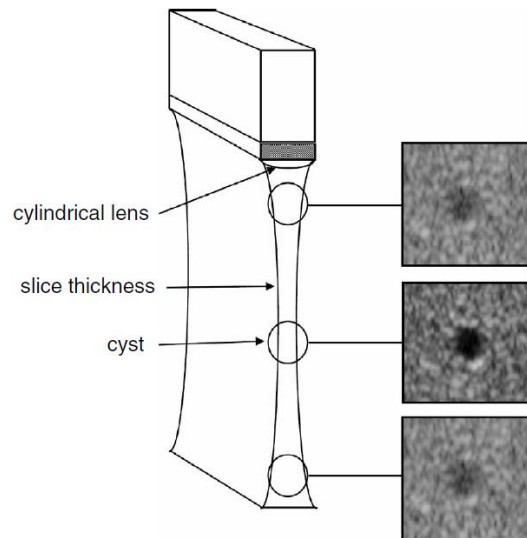
B-Mode Image Properties

□ Lateral Resolution



□ Thickness resolution

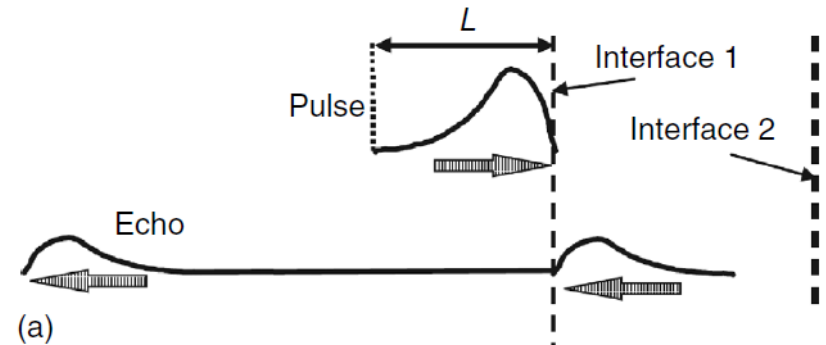
▣ Elevation



B-Mode Image Properties

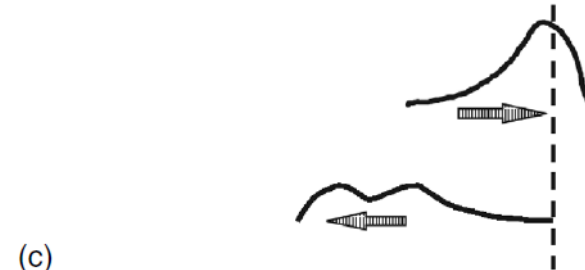
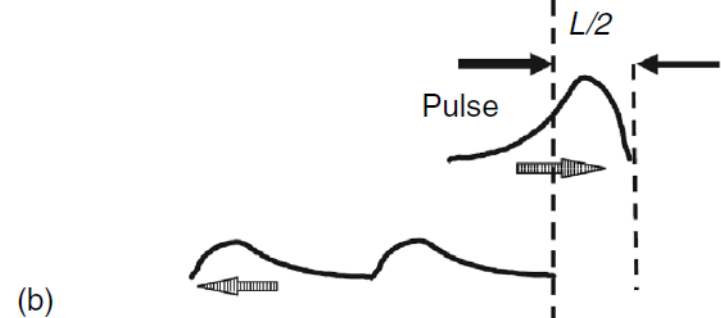
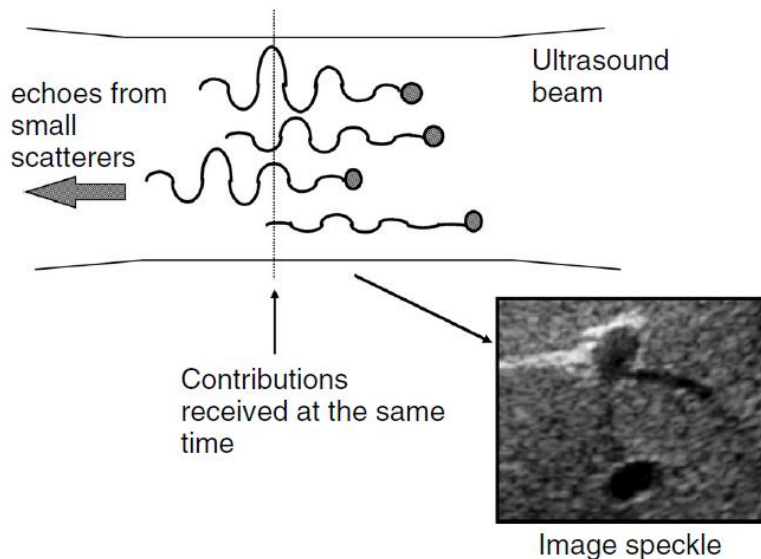
- Axial resolution

- ▣ Half pulse length



- Speckle

- ▣ Random yet stationary pattern

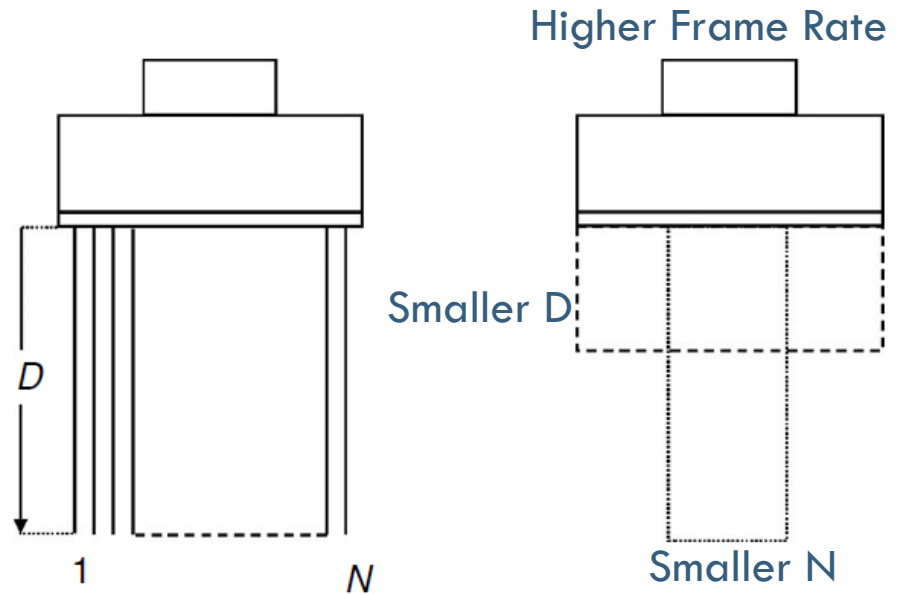


B-Mode Image Properties

- Frame time / Frame rate
 - ▣ Time to scan a complete image

$$\text{frame time} = 2DN/c$$

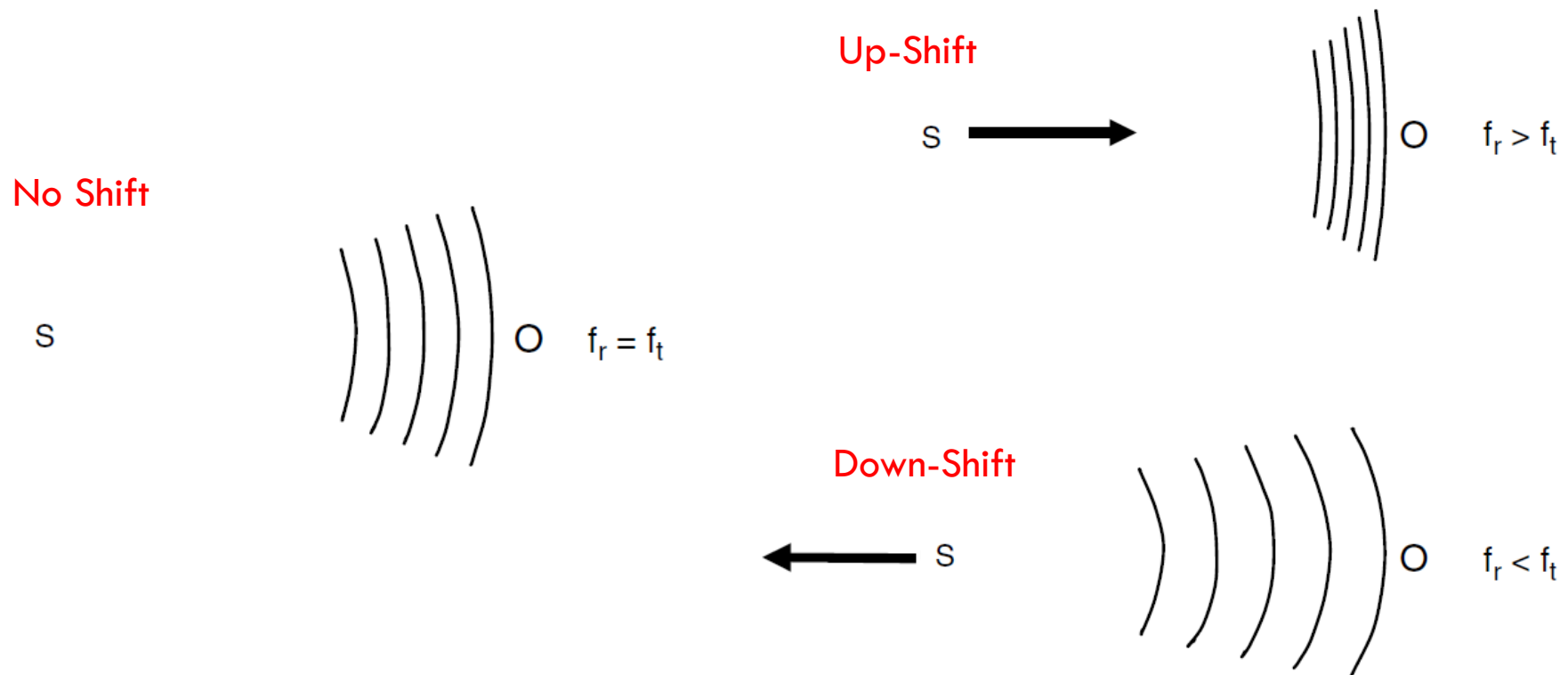
$$\text{frame rate} = (c/2DN)$$



- ▣ Example: time to scan 1 cm = $2 \times 1 \text{ cm} / c = 2 \text{ cm} / (1540 \text{ m/s}) = 13 \mu\text{s}$
Then, frame time to scan a 20 cm depth with 128 lines = $13 \mu\text{s} \times 20 \times 128$
Frame rate = $1 / \text{frame time} = 30 \text{ frames/s}$

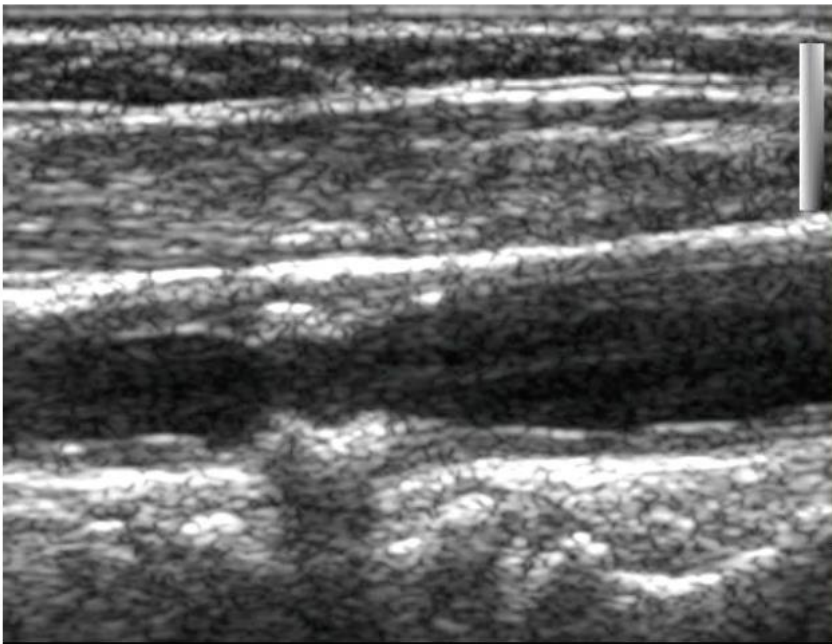
Doppler Ultrasound

- **Doppler effect:** Change in the observed frequency of the sound wave compared to the emitted frequency which occurs due to relative motion between observer and source

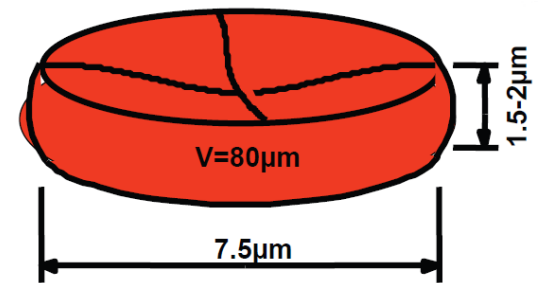


Doppler Ultrasound

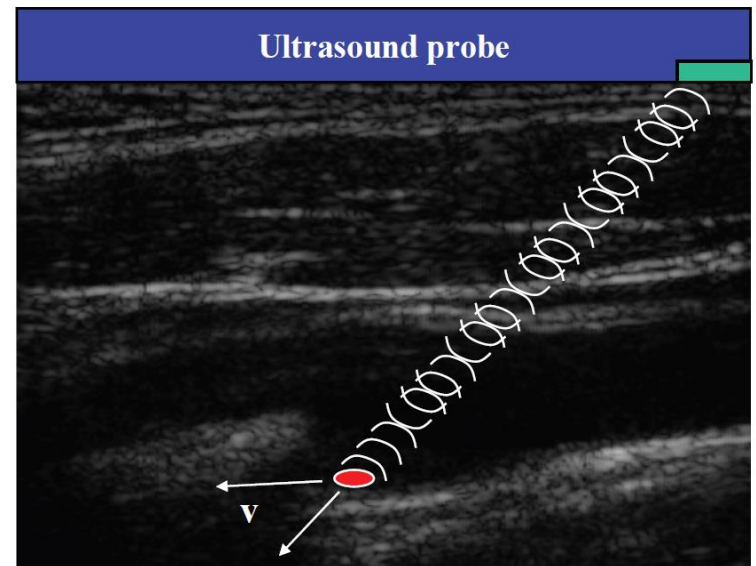
- RBCS in blood are hardly visible in ultrasound images
 - ▣ Scattering because of its very small size



Carotid artery with calcified plaque



Red blood cell



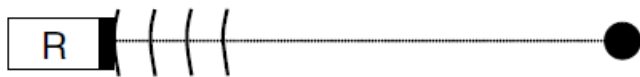
Doppler Ultrasound

□ Doppler Shift Equation

$$f_d = f_r - f_t = \frac{2f_t v \cos \theta}{c}$$



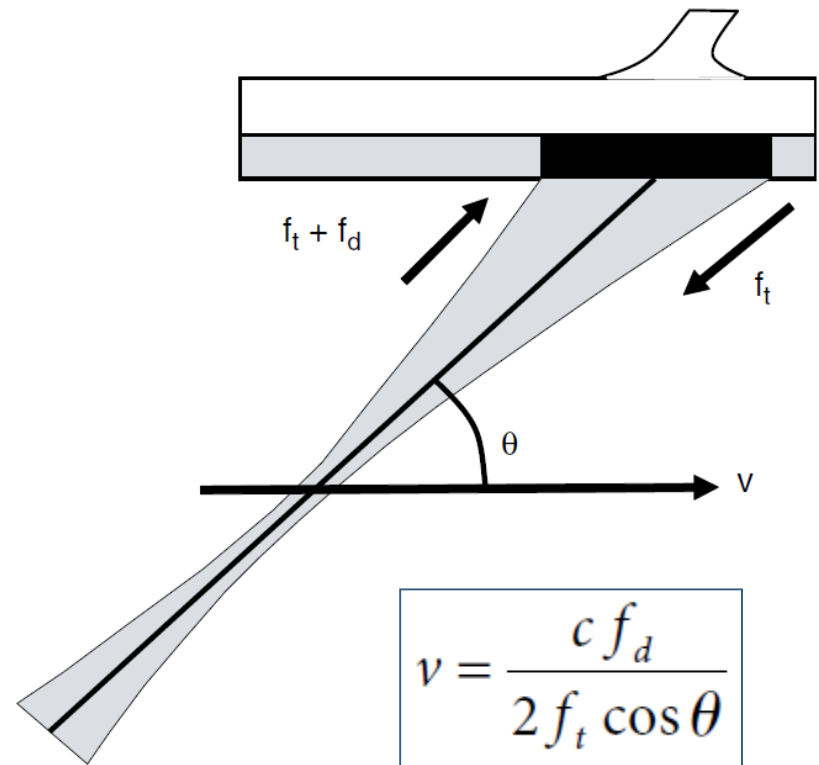
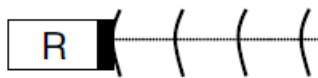
$$f_r = f_t$$



$$f_r > f_t$$



$$f_r < f_t$$

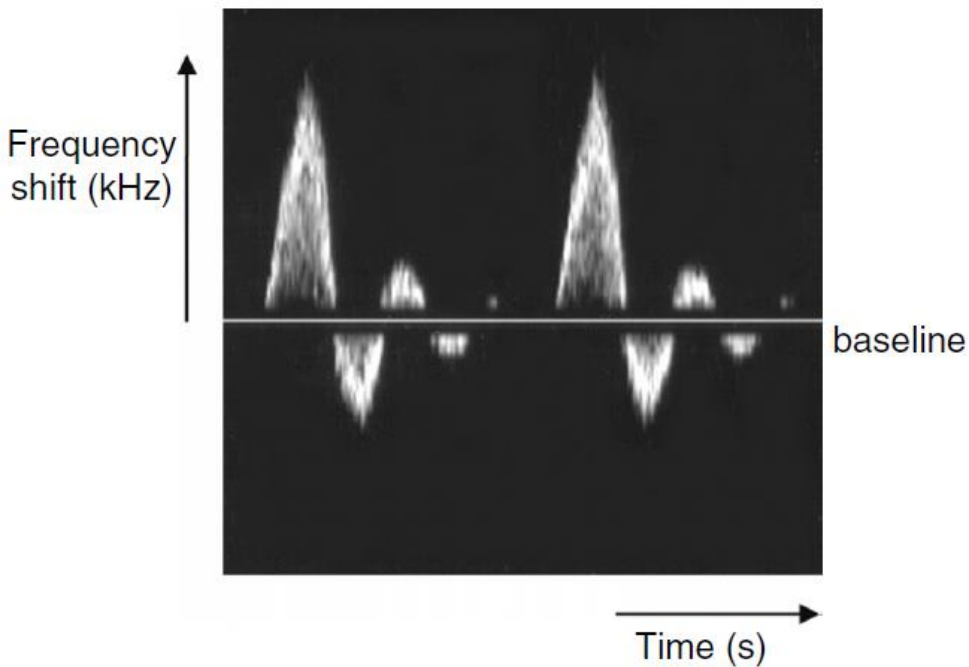


$$v = \frac{c f_d}{2 f_t \cos \theta}$$

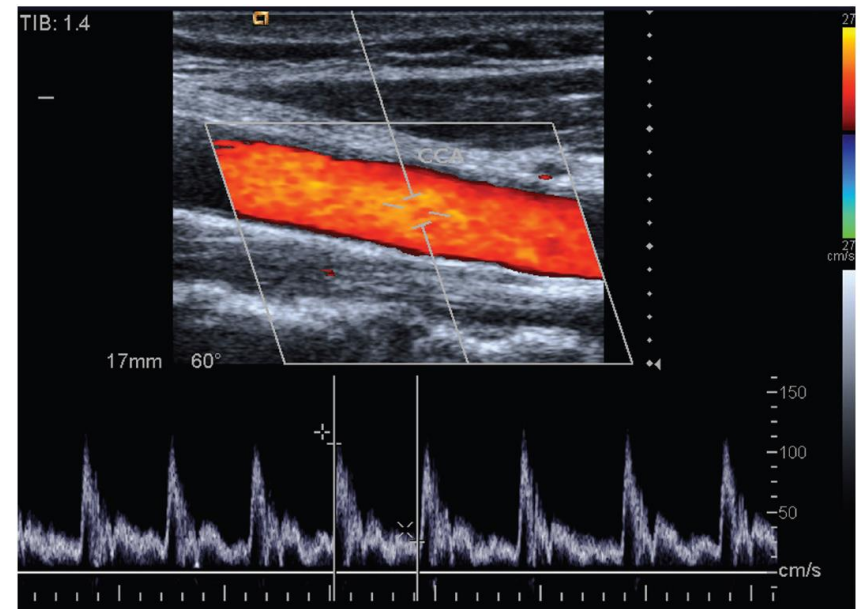
Doppler Ultrasound

- Doppler display modes

Spectral Doppler

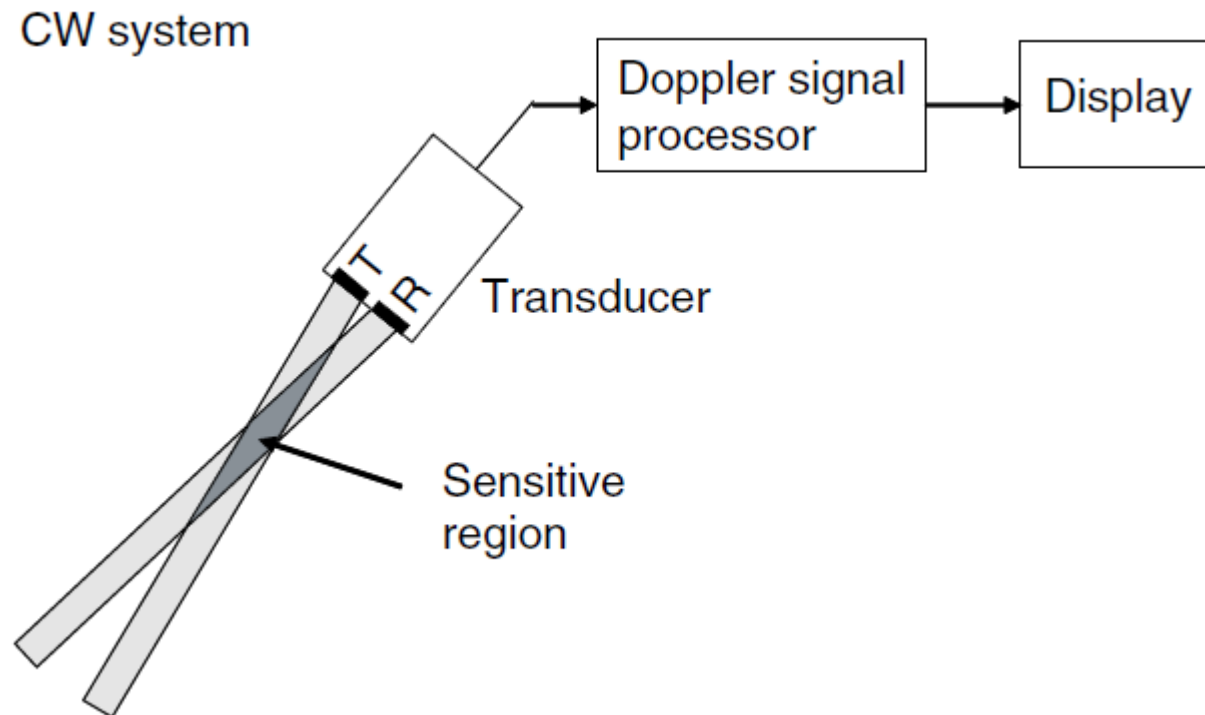


Color Doppler



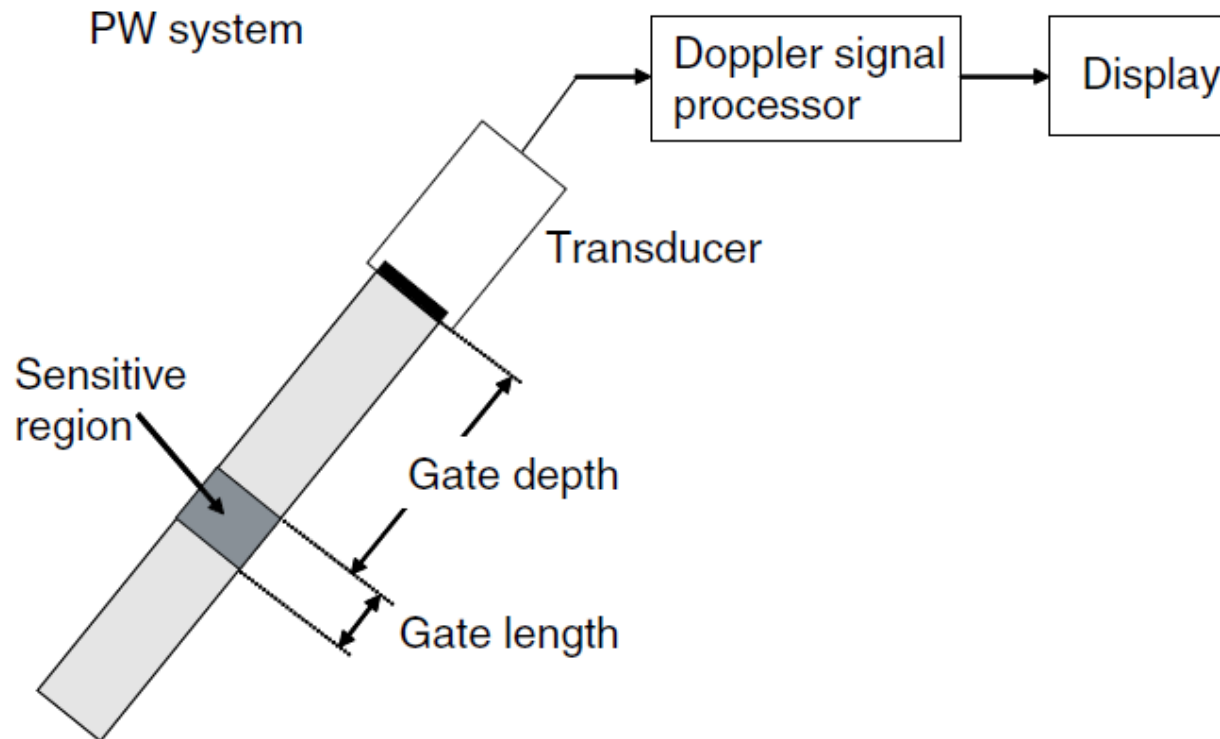
Doppler Ultrasound

- Continuous Wave (CW) Doppler
 - ▣ Only a small region for Doppler sensitivity
 - ▣ No range information
 - ▣ No limitation on maximum velocity and high velocity accuracy



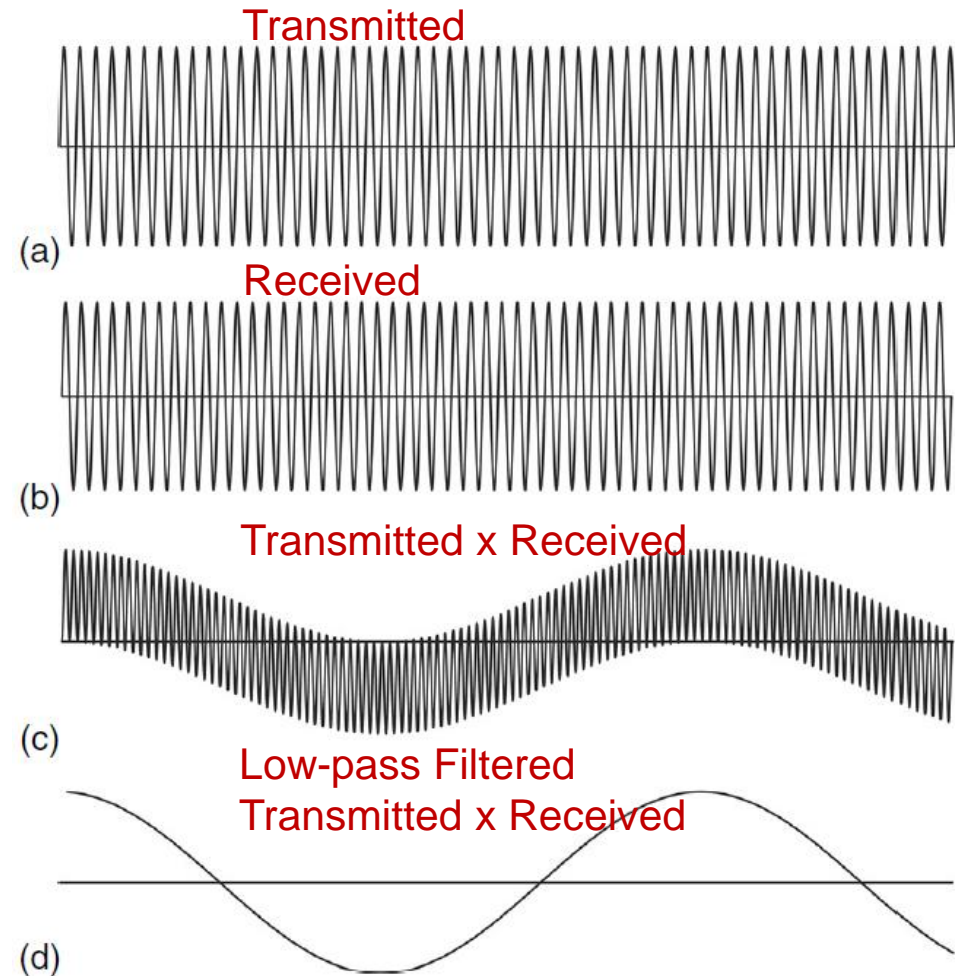
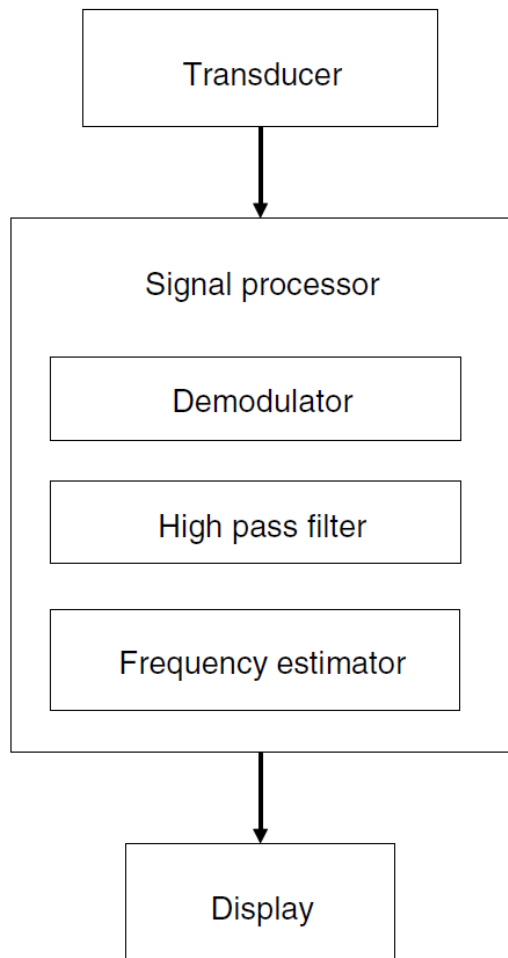
Doppler Ultrasound

- Pulsed-Wave (PW) Doppler
 - ▣ Range information is available and region is selectable by user
 - ▣ Limitations on maximum velocity and accuracy



Doppler Ultrasound

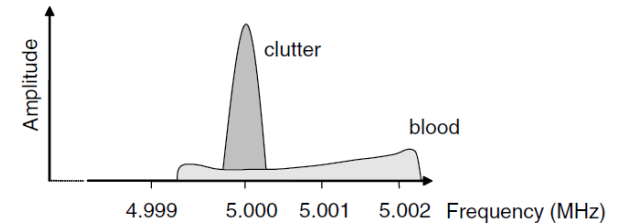
□ CW Signal Processing



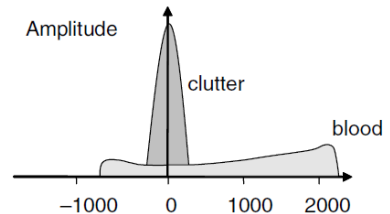
Doppler Ultrasound

- Clutter: signal from stationary tissues
 - ▣ Low Doppler shift and much stronger signal
 - ▣ Signal from stationary tissue and wall motion
 - ▣ Critical step in Doppler processing

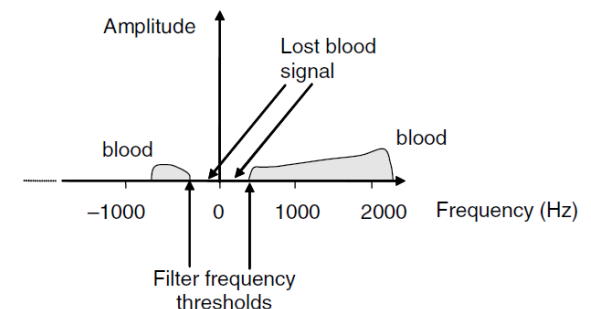
	Velocity ranges	Signal intensity
Blood	0–600 cm s ⁻¹	Low
Tissue	0–10 cm s ⁻¹	40 dB higher than blood



Demodulation



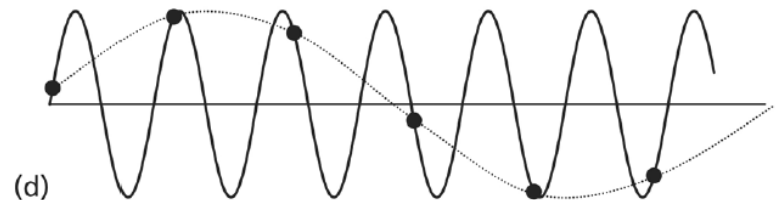
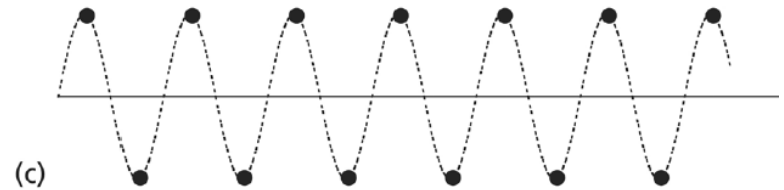
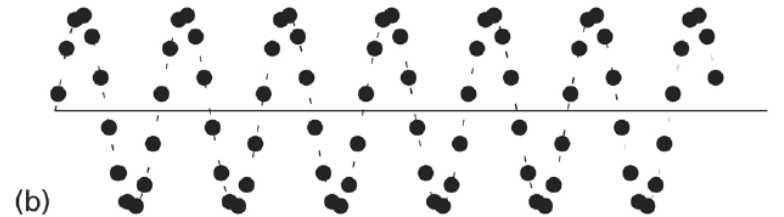
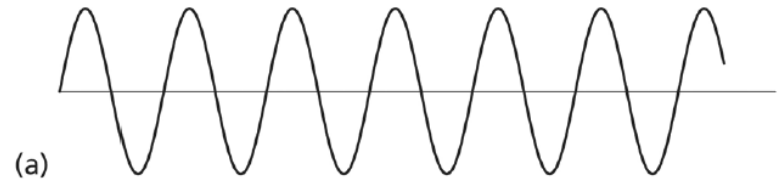
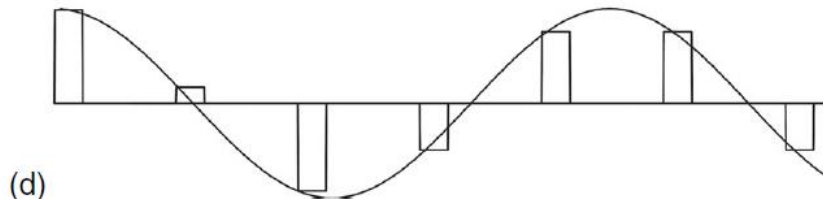
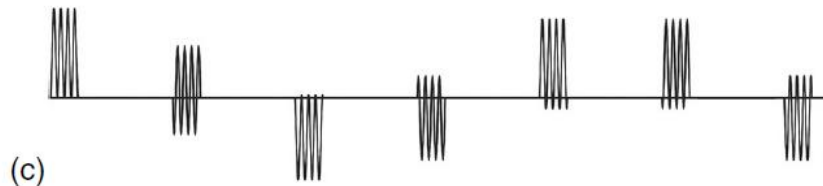
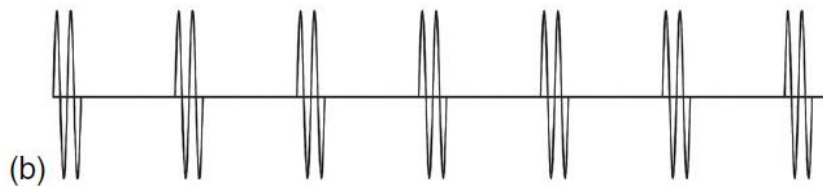
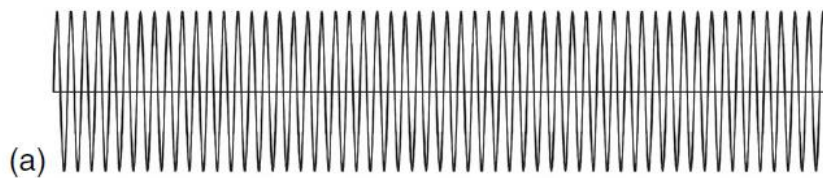
High pass filter



Doppler Ultrasound

□ PW Doppler processing: Sampled version of CW Doppler

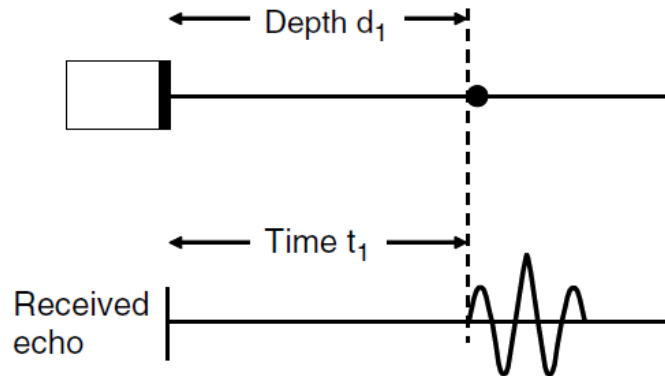
▣ Aliasing may occur



Doppler Ultrasound

□ Time-domain PW processing techniques

(a) First pulse, time t_1

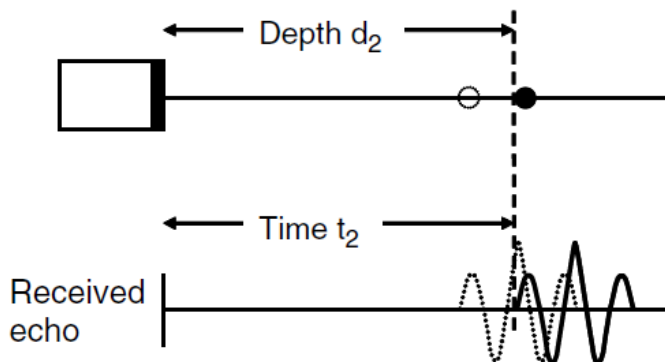


$$d_1 = c t_1 / 2, \quad d_2 = c t_2 / 2$$

$$d_m = d_2 - d_1$$

$$d_m = c(t_2 - t_1) / 2$$

(b) Second pulse, time t_2



$$\text{PRI} = t_2 - t_1 \quad \text{PRI} = 1/\text{PRF}$$

$$v = d_m / \text{PRI} = (t_2 - t_1) c \text{PRF} / 2$$

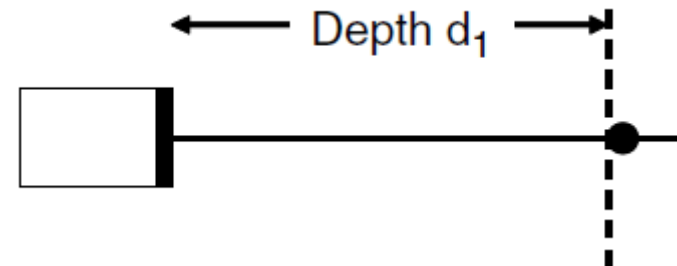
Doppler Ultrasound

- Example: Consider Doppler imaging of a vessel at depth $d_1 = 10$ cm. derive the maximum detectible velocity if the transmitted signal frequency was 5 MHz and Doppler angle was 45° .

Time to collect one sample = PRI = $13 \mu\text{s}/\text{cm} \times (10 \text{ cm}) = 130 \mu\text{s}$

Sampling frequency = PRF = $1/\text{PRI} = 7692 \text{ Sa/s} = 2 f_d^{\text{max}}$

$$v = \frac{c f_d}{2 f_t \cos \theta} \quad \longrightarrow \quad v_{\text{max}} = (1540 \times 7692 / 2) / (2 \times 5 \times 10^6 \times \cos(45^\circ))$$

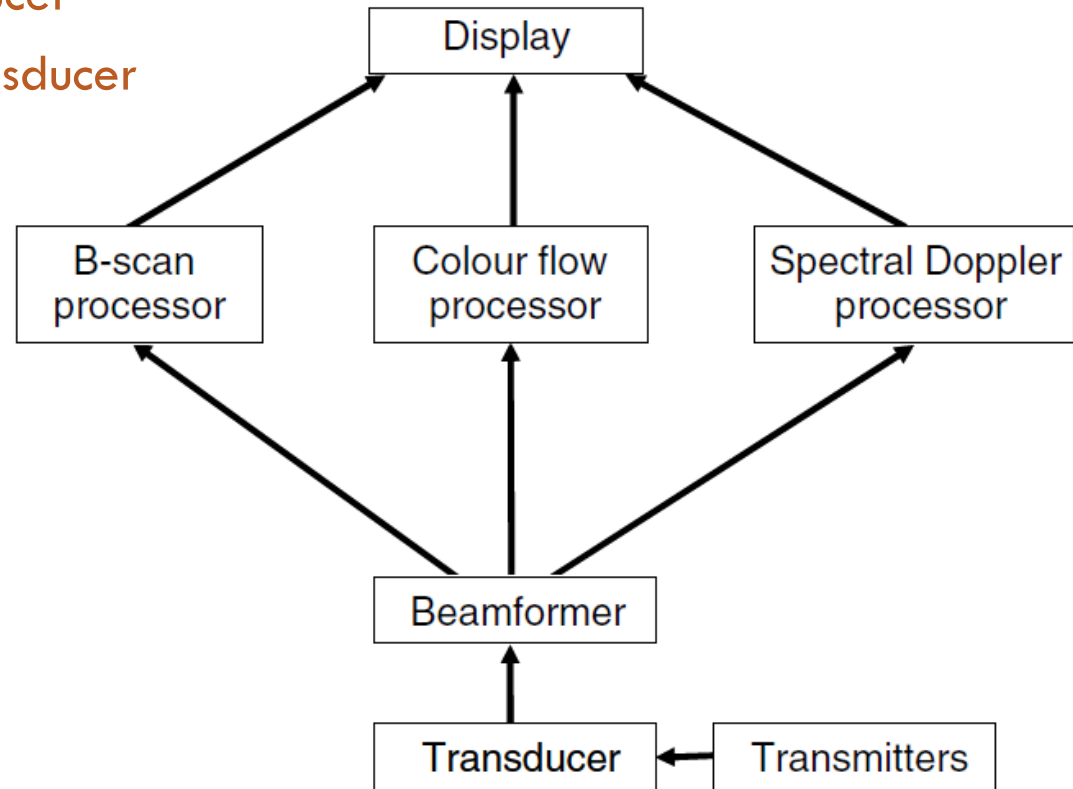
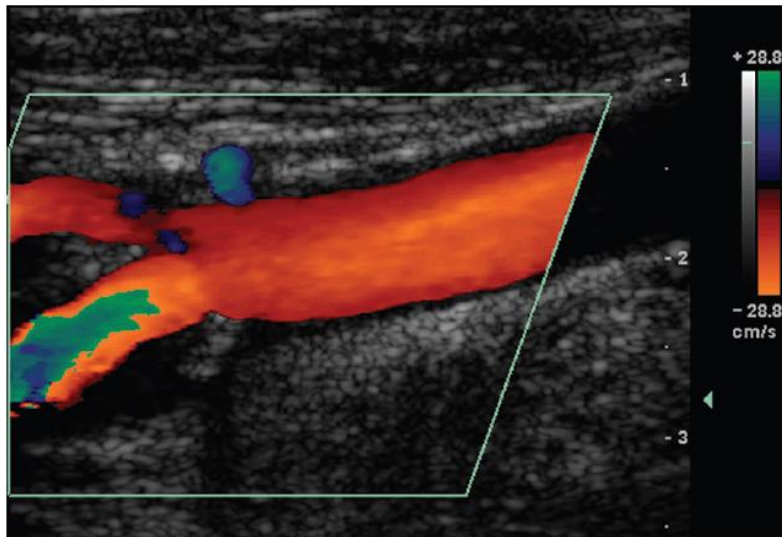


Doppler Ultrasound

- Aliasing
 - ▣ Highest Doppler frequency shift that can be measured is equal to $PRF/2$
- Angle dependence
 - ▣ Estimated Doppler shift is dependent on cosine of the angle between the beam and the direction of motion
- Clutter breakthrough
 - ▣ Tissue motion giving rise to Doppler frequencies above wall thump or clutter filter may be displayed on spectral Doppler or color flow systems
- Loss of low Doppler
 - ▣ Blood velocities which give rise to low Doppler frequencies (as a result of low velocity or angle near to 90°) will not be displayed if value of Doppler frequency is below the level of wall thump or clutter filter

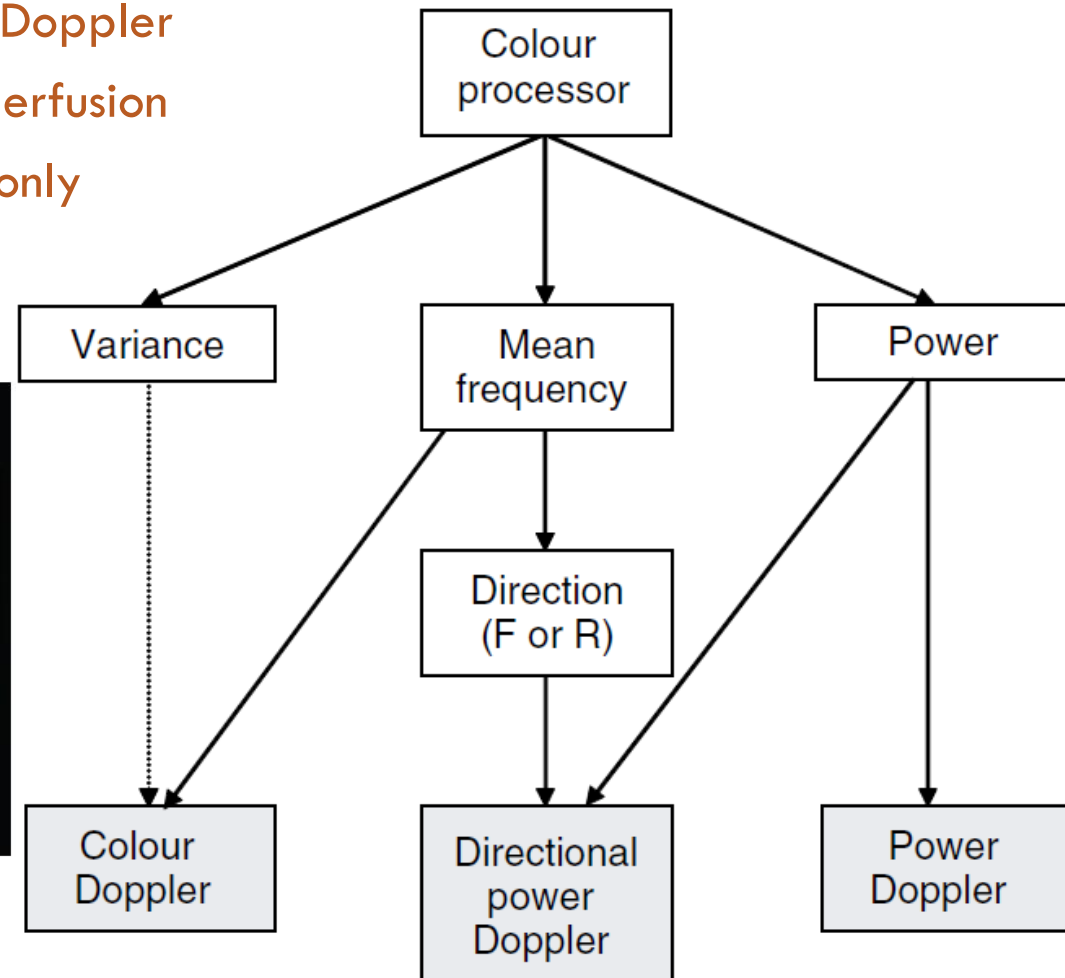
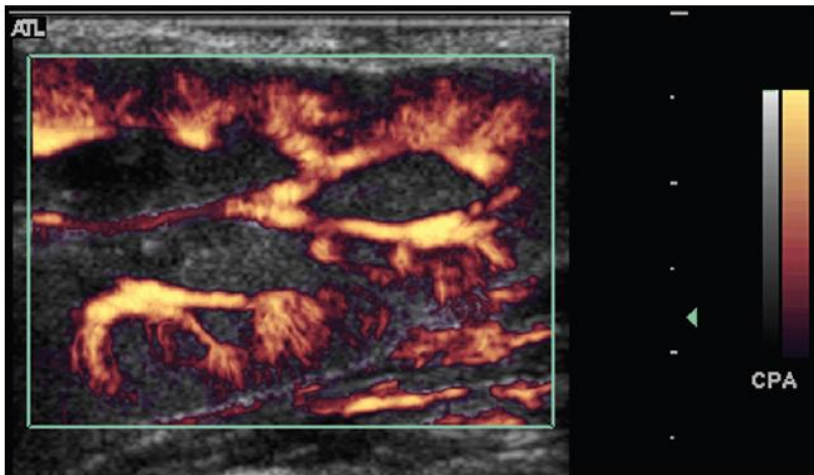
Color Doppler

- Maps mean blood velocity at each points and encodes it in color on the usual B&W ultrasound image
 - ▣ Red: flow toward transducer
 - ▣ Blue floe away from transducer



Power Doppler

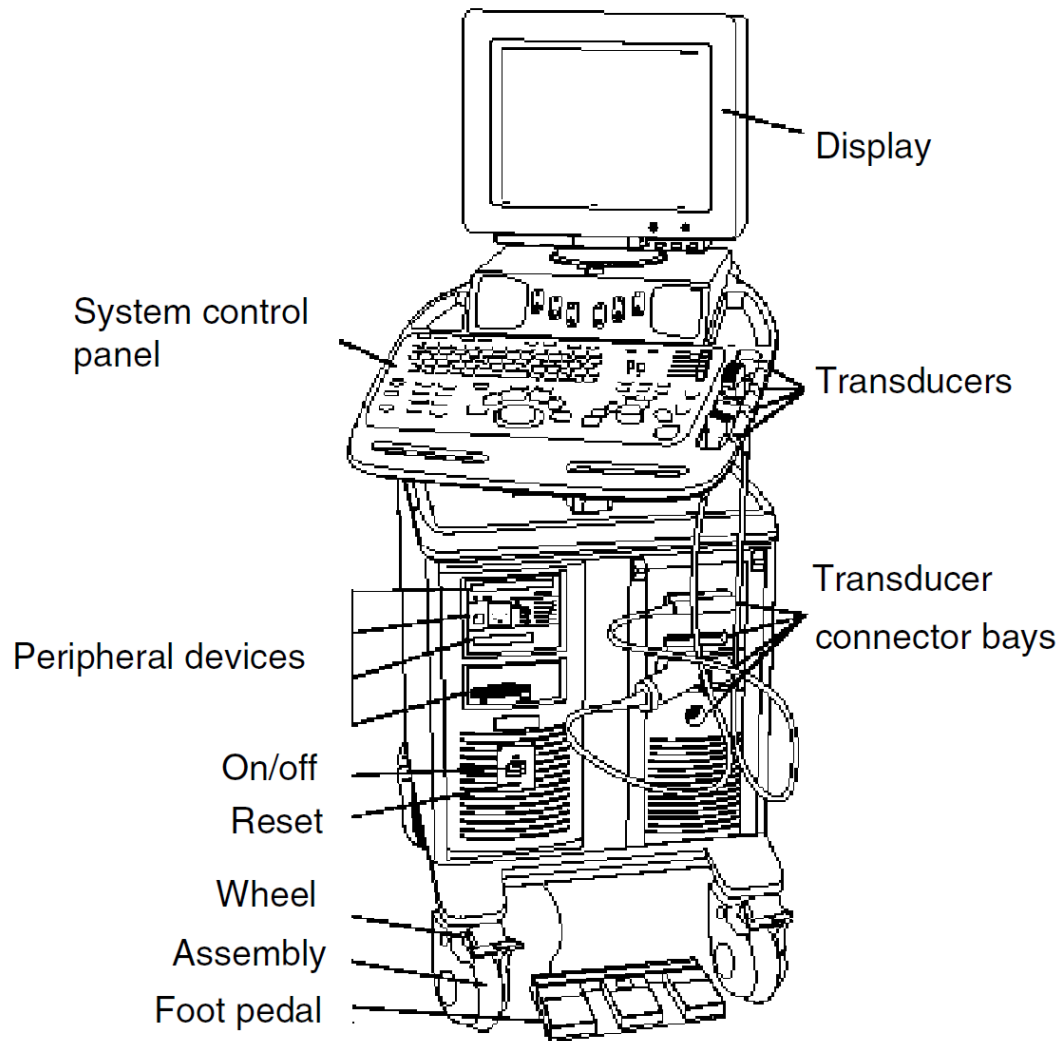
- Estimate of the power of all shifted components
 - ▣ Not just mean like in color Doppler
 - ▣ Very useful for assessing perfusion
 - ▣ Encoded in shades of red only



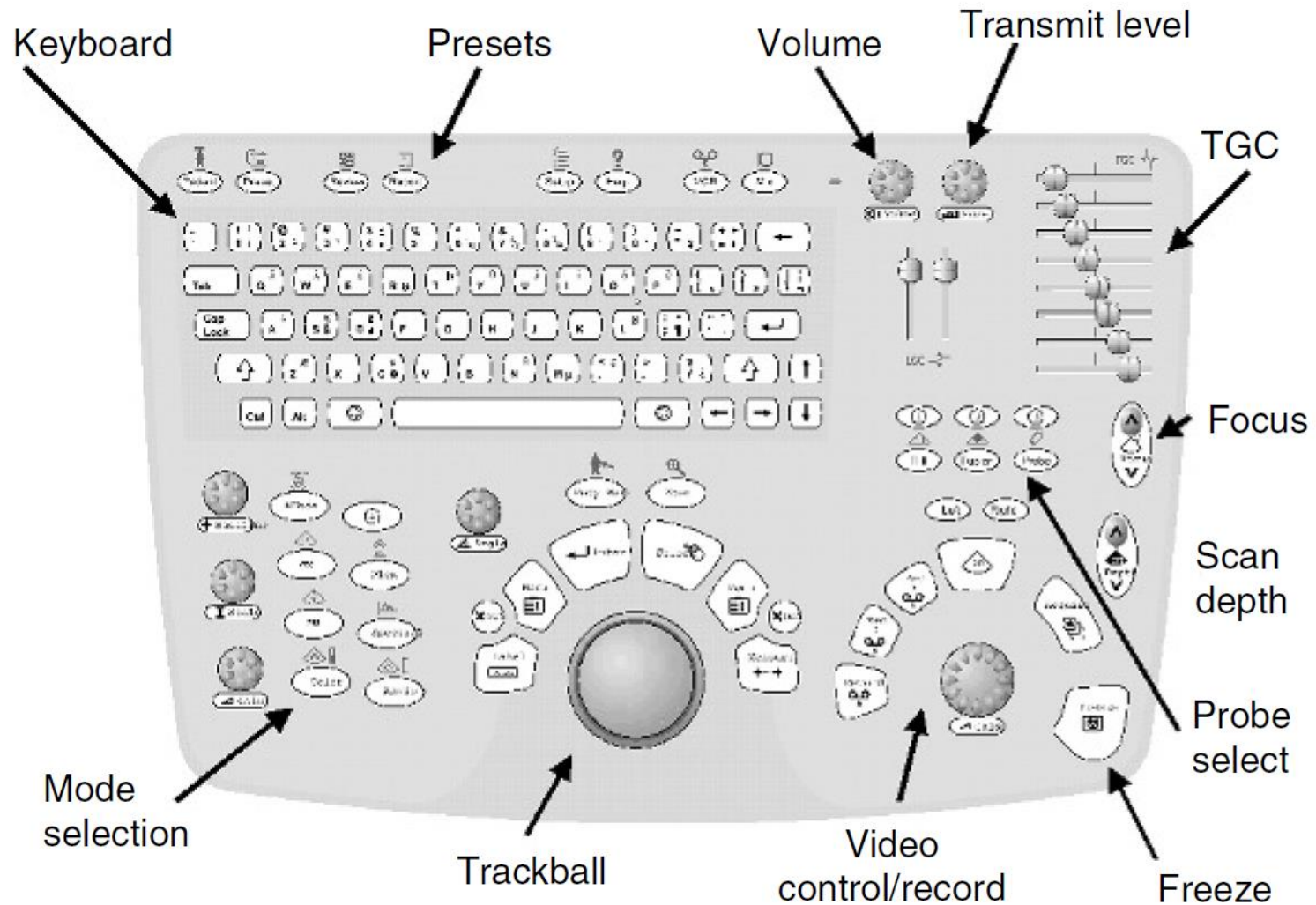
Ultrasound Safety

- A fundamental approach to the safe use of diagnostic ultrasound is to use the lowest output power and the shortest scan time consistent with acquiring the required diagnostic information
 - ▣ “ALARA” principle (i.e. as low as reasonably achievable)

Ultrasound Imaging System: External Look



Keyboard Controls



Covered Material and Suggest Problems

- Chapter 2: problems 3, 4, 5, 7, 10
- Chapter 3: problems 1, 2, 3, 4, 5, 6, 7, 8, 9, 10
- Chapter 4: problems 1, 2, 3, 4, 5
- Chapter 7: problems 3, 4, 5, 6, 7, 8
- Consider Doppler blood flow velocity estimation in a vessel at depth of 5 cm and angle of 60° . Find out whether aliasing will occur when estimating blood velocity if the actual velocity in that vessel is 50 cm/s. Let the transmitted signal frequency be 7 MHz.