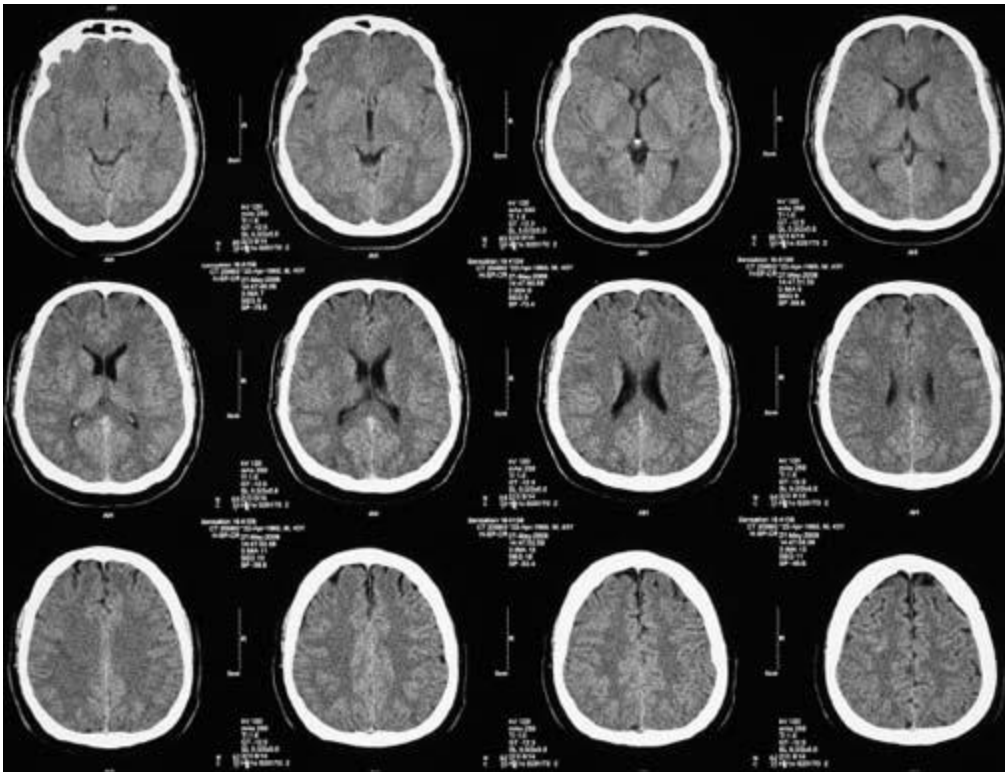


MEDICAL EQUIPMENT II - 2011

COMPUTED TOMOGRAPHY

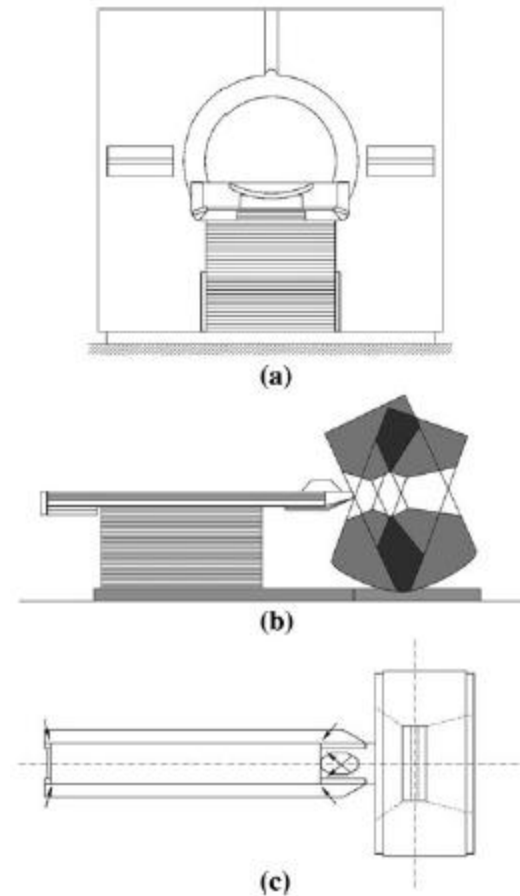
Computed Tomography

- X-ray based imaging method
- Main feature: sectional imaging rather than projection imaging



Computed Tomography Components

- **Gantry** with a central opening, into which the patient is moved during the examination.
- **X-ray tube**, the source of the X-rays that pass through the body situated in the gantry in the form of a series of projections;
- **Detector** array converts the projection values, in the form of radiation intensities, into electrical quantities. Usually, the whole detector array rotates synchronously with the X-ray tube around the test object
- **Table** allows the patient to be maneuvered easily into position

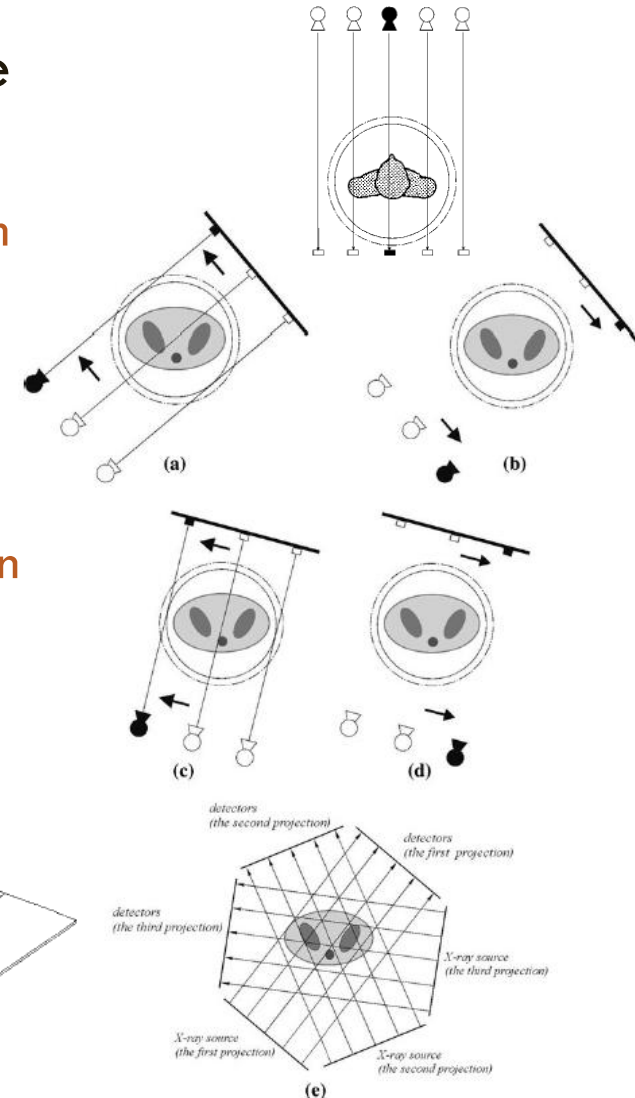
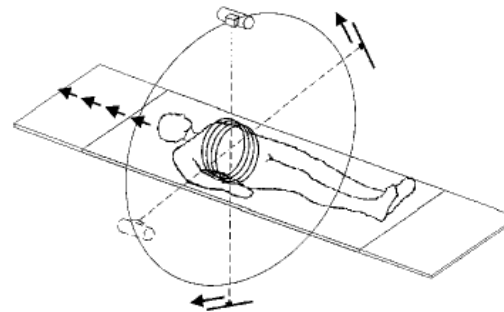


CT Scanner Design

- One of three basic tube-detector projection systems
- A projection system using a parallel beam of radiation
 - ▣ Parallel-beam system
- A system using a beam of radiation in the shape of a fan
 - ▣ Fan-beam system
- A system using a beam of radiation in the shape of a cone
 - ▣ Cone-beam system

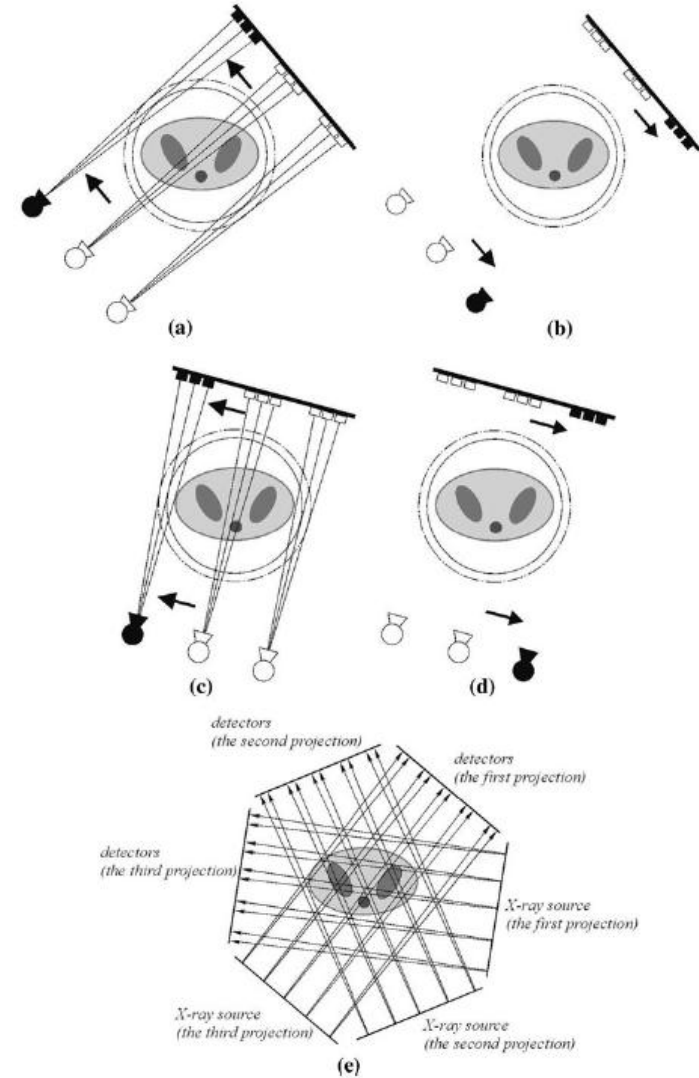
First-Generation CT Scanners

- Pencil beam or translation/rotation single detector CT scanners
 - ▣ belong to the parallel-beam projection system
- Two components to the movement of the rigidly coupled tube-detector system
 - ▣ lateral movement to make a single projection
 - ▣ circular movement about the central opening in the gantry to gather all projections necessary to form the image
- Very slow (5 min/slice)



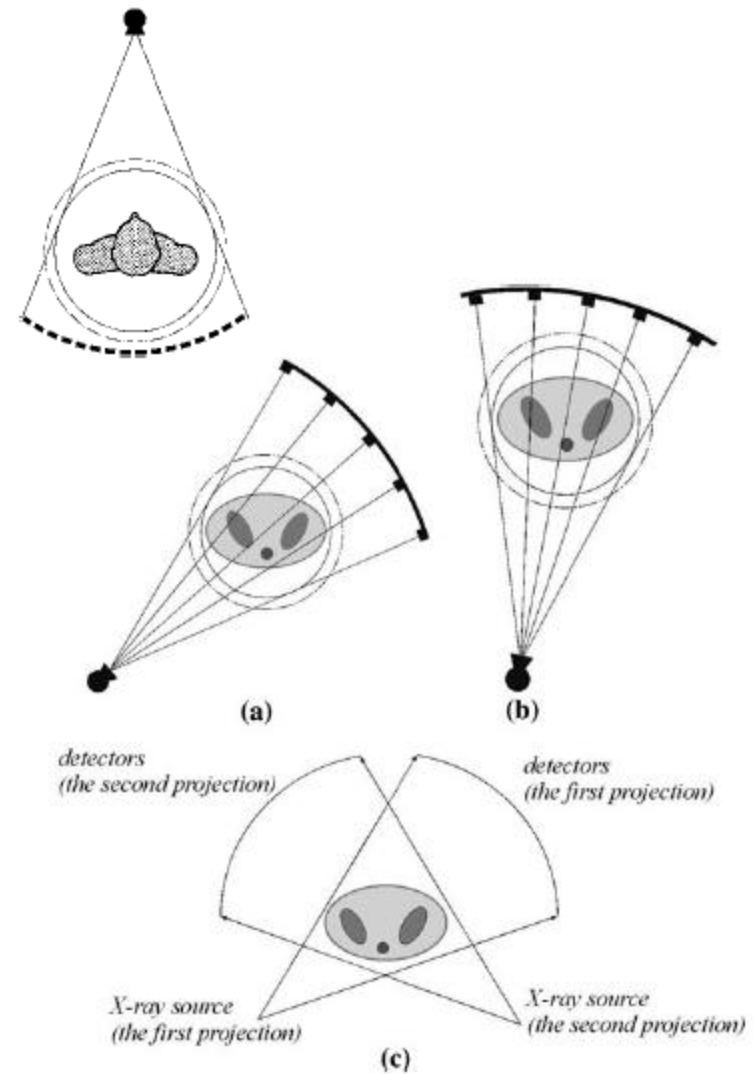
Second-Generation CT Scanners

- Partial fan beam or translation/rotation multiple detector scanners
- 3-52 detectors in the array
 - ▣ enable the projections to cover a larger area of the patient's body at any one time
 - ▣ results in reduction of number of projections needed to reconstruct an image
 - ▣ Faster!



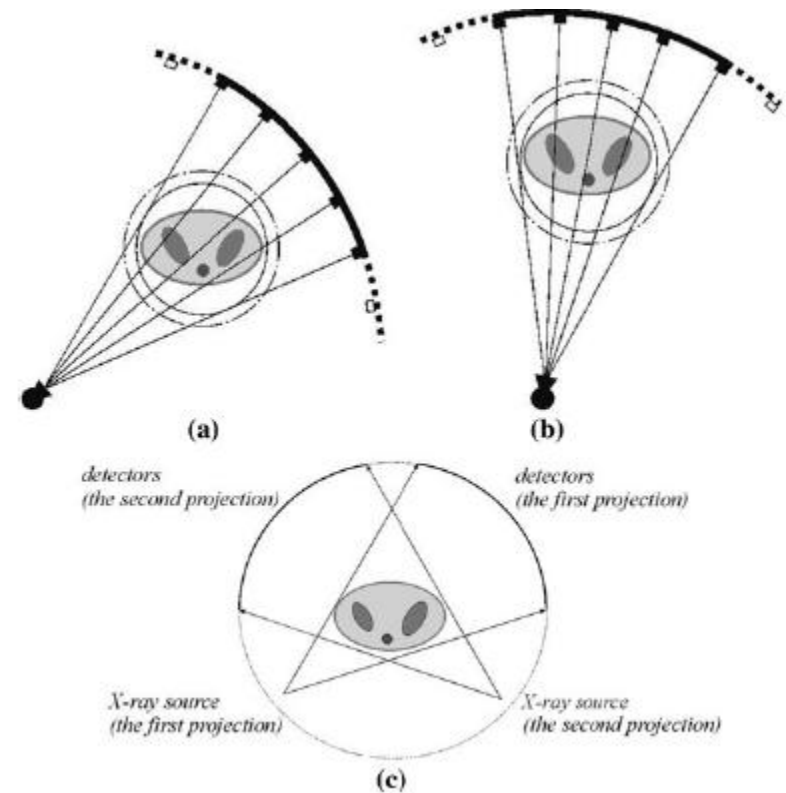
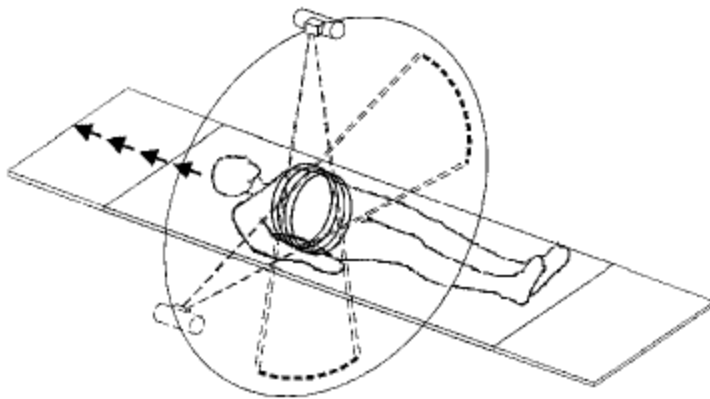
Third-Generation CT Scanners

- Elimination of lateral movement of tube-detector system
- Fan-beam or continuous rotation scanner
 - ▣ Fan beam of radiation (40-55 degrees) to encompass whole object
- Increase number of detectors in the array moving synchronously with rotating X-ray tube (up to 1,000 detectors)
- Much faster: 5 s/slice



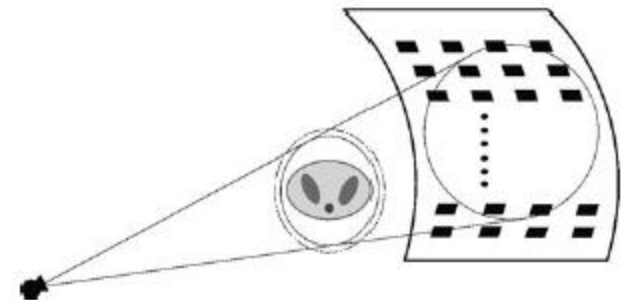
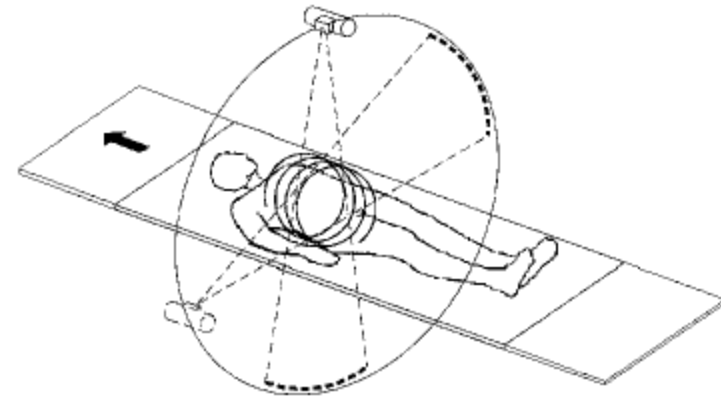
Fourth-Generation CT Scanners

- Differ only slightly from the third generation
 - ▣ Rotation of the detector array is eliminated by arranging it on a stationary ring
 - ▣ “Rotate-fixed” scanner



Spiral Scanners

- Fan beam scanning + table motion
- Single-slice spiral CT scanner (SSCT)
- Multi-slice spiral CT (MSCT)
 - ▣ 8-34 rows of detectors
- Cone beam spiral CT (CBCT)
 - ▣ possible to increase width of detector array to 16 or even 320 elements
 - ▣ Allowing simultaneous acquisition of up to 256 adjacent image slices
 - ▣ No collimation losses: less x-ray power
 - ▣ Faster, higher resolution scanning



Hounsfield Units

- It is common practice in medical applications to use units on the Hounsfield scale: Hounsfield units (HU) .
 - Value usually varies in the range -1,000 (air) to 3,000 (bone), making it necessary to apply a so-called window (center C and width W).

$$\text{CT number} = 1000 \frac{(\mu - \mu_w)}{\mu_w}$$

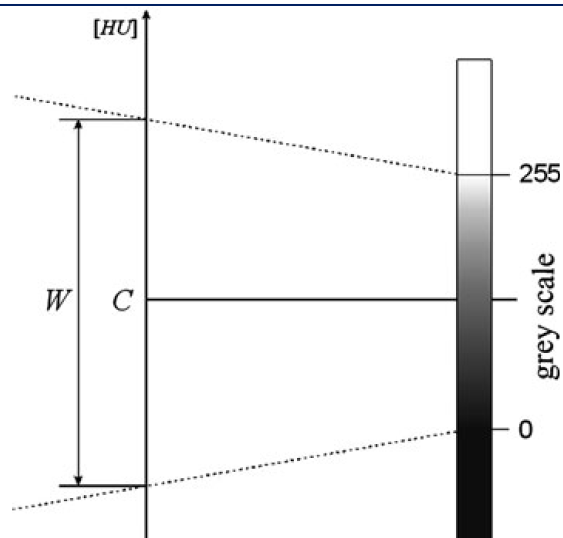
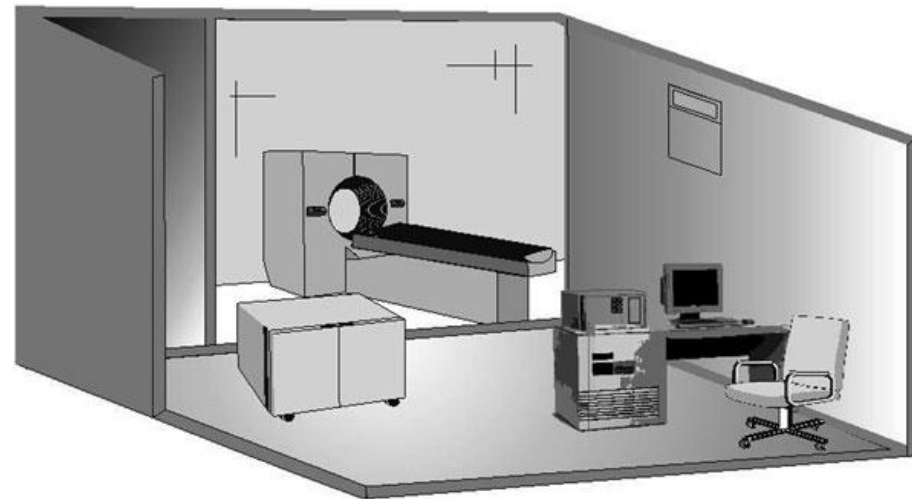
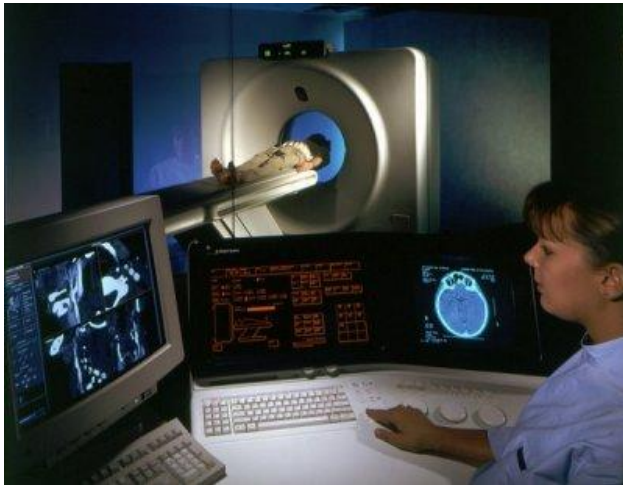


Fig. 3.41 The same slice viewed with different values of window parameters: the left image with the pulmonary window ($C = -600$, $W = 1,600$), the right image with the mediastinal window ($C = 50$, $W = 350$)

CT Installation

- CT room must meet several requirements
 - ▣ it must have floors with adequate load-carrying capacity
 - ▣ its walls must be constructed of X-ray absorbing material (this is usually a barium (Ba) plaster)
 - ▣ the floor should be lined with material that is both anti-slip and antistatic
- Separate rooms for CT scanner and radiographers;
 - ▣ Separated by special protective window-glass (containing lead, Pb)



CT Scanner Physical Elements

- A CT scanner consists of the following main elements
 - ▣ a data acquisition system that carries out the X-ray projections
 - ▣ a computer to reconstruct the images from the projections and to assist in the analysis of the reconstructed images
 - ▣ a variable power supply
 - ▣ a monitor to display the routine operation of the computer system and to act as an interactive interface in the diagnosis of reconstructed images
 - ▣ a documentation camera to produce an image on film similar to traditional X-ray images
 - ▣ other data archiving systems, such as tape or disk, collectively referred to as storage devices

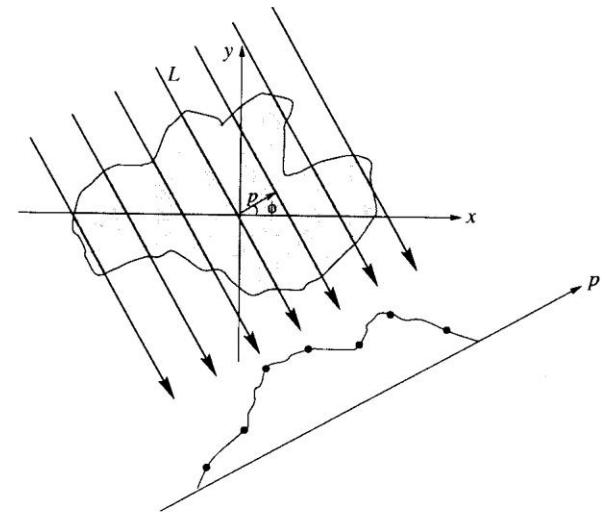
Image Reconstruction Problem

- For an $N \times N$ image, we have N^2 unknowns to estimate
 - ▣ Sufficient equations must be available
 - ▣ In most cases the problem can be formulated as a linear system
 - ▣ Simplest case when the acquired data correspond directly to the image points (i.e., diagonal linear system matrix), e.g., ultrasound imaging.



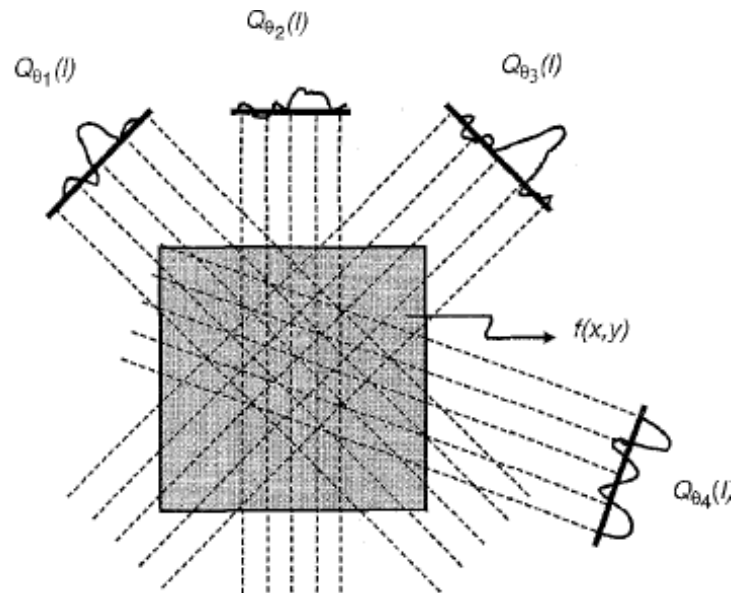
Conventional Projection Imaging

- The image points represents the line integral of the tissue property along the incident ray
 - ▣ Plain x-ray imaging
 - ▣ Difficulty to discern overlapping structures along projection ray
- Question: Can we gain more information by projecting in different directions?
 - ▣ Different directions provide different equations about the different parts of the image
 - ▣ How many directions are needed?



Computed Tomography: Reconstruction from Projections

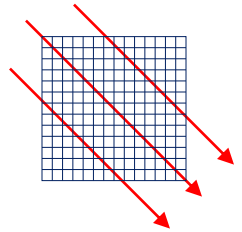
- Collects data from projections at different angles and attempts to construct a “cross-section” that resolves the location ambiguity present in projection images
- Example: X-ray computed tomography



Mathematical Formulation

- Let image points be expressed as $I(x,y)$
- The projection data at an angle θ can be expressed as,

$$P_{\theta}(\rho) = \sum_{x,y} \alpha_{\rho}^{\theta}(x,y) \cdot I(x,y)$$

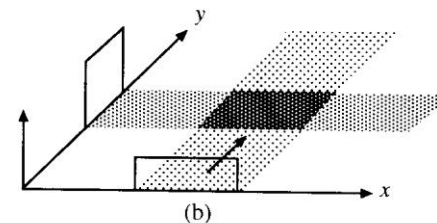
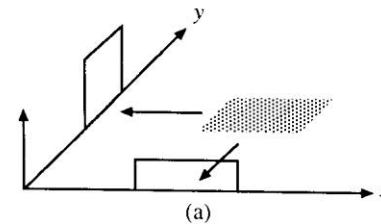
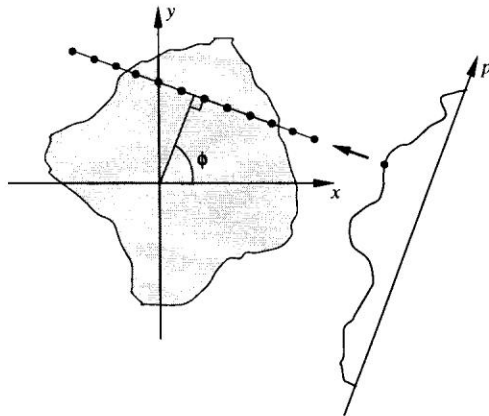


- From all projections, a linear system representation of the problem can be constructed as,

$$\begin{bmatrix} P_{\theta_1}(\rho_1) \\ P_{\theta_1}(\rho_2) \\ \vdots \\ P_{\theta_n}(\rho_m) \end{bmatrix} = \vec{P} = \begin{bmatrix} \alpha_{\theta_1}^{\rho_1}(x_1, y_1) & \alpha_{\theta_1}^{\rho_1}(x_1, y_2) & \cdots & \alpha_{\theta_1}^{\rho_1}(x_N, y_N) \\ \alpha_{\theta_1}^{\rho_2}(x_1, y_1) & \alpha_{\theta_1}^{\rho_2}(x_1, y_2) & \cdots & \alpha_{\theta_1}^{\rho_2}(x_N, y_N) \\ \vdots & \vdots & \cdots & \vdots \\ \alpha_{\theta_n}^{\rho_m}(x_1, y_1) & \alpha_{\theta_n}^{\rho_m}(x_1, y_2) & \cdots & \alpha_{\theta_n}^{\rho_m}(x_N, y_N) \end{bmatrix} \cdot \begin{bmatrix} I(x_1, y_1) \\ I(x_1, y_2) \\ \vdots \\ I(x_N, y_N) \end{bmatrix} = A \cdot \vec{I}$$

Back-Projection Method

- Start from a projection value and back-project a ray of equal pixel values that would sum to the same value
- Back-projected ray is added to the estimated image and the process is repeated for all projection points at all angles
- With sufficient projection angles, structures can be somewhat restored

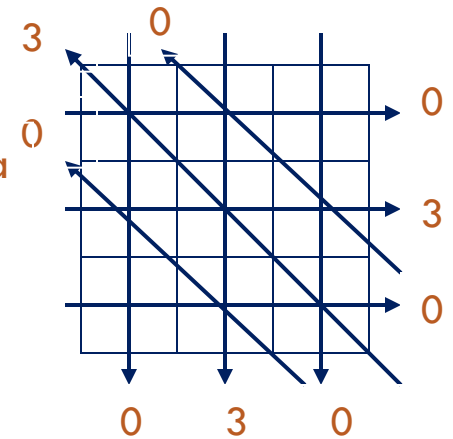


Back-Projection Example

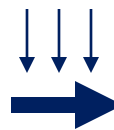
True
Image

0	0	0
0	3	0
0	0	0

Projection Data



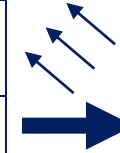
0	0	0
0	0	0
0	0	0



0	1	0
0	1	0
0	1	0



0	1	0
1	2	1
0	1	0



1	1	0
1	3	1
0	1	1

Initial
Solution



Iterate until sufficient accuracy is achieved



Algebraic Reconstruction Technique (ART)

- A low-complexity iterative solver to the algebraic reconstruction problem
- Starts with an initial estimate and tries to push the estimate closer to the true solution
 - ▣ Instead of back-projecting the average ray value, the error between the projection computed from current estimate and the true is used

$$Update = P_{\theta}(\rho) - \sum_{x,y} \alpha_{\rho}^{\theta}(x,y) \cdot \hat{I}(x,y)$$

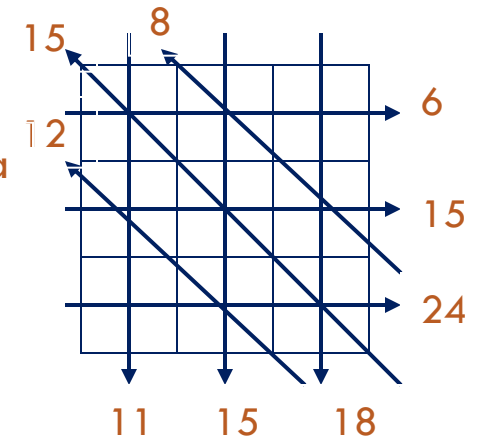
ART Example

True

1	2	3
4	5	6
7	8	9

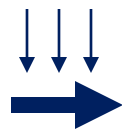
Image

Projection Data



0	0	0
0	0	0
0	0	0

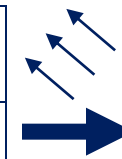
Initial
Solution



4	5	6
4	5	6
4	5	6



1	2	3
4	5	6
7	8	9



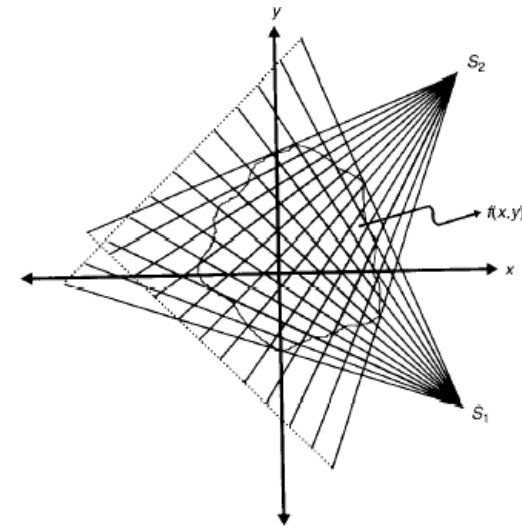
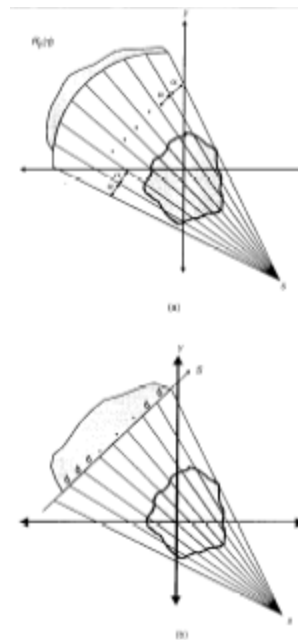
1	2	3
4	5	6
7	8	9

Iterate until sufficient accuracy is achieved



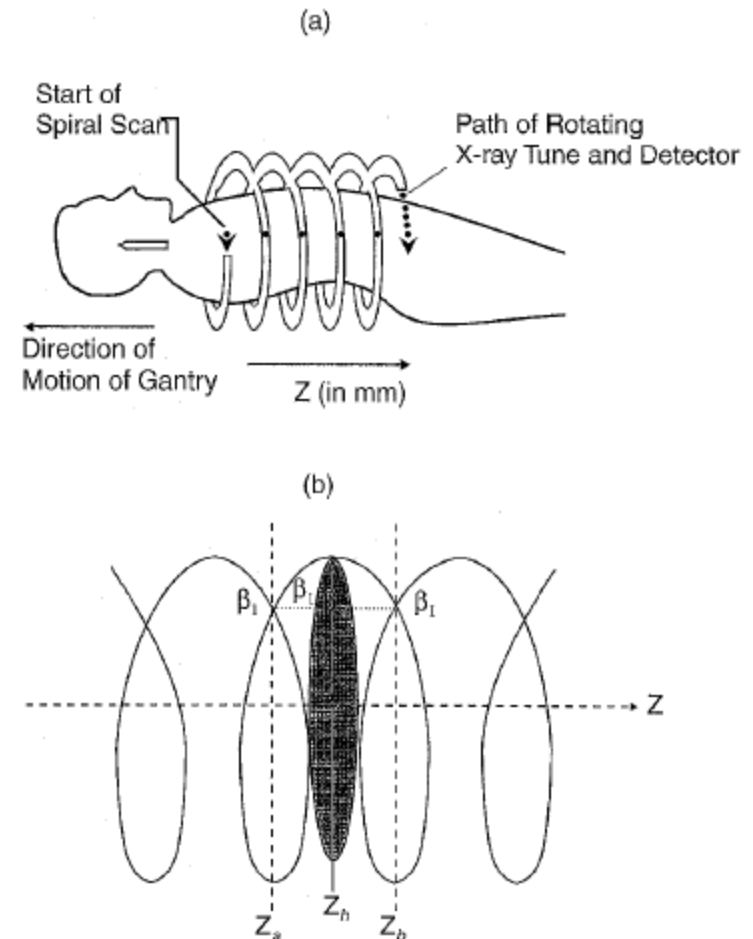
Problem Extensions: Fan Beam Problem

- In newer CT generations, fan beams are used to gain more efficiency in hardware implementation
- Detectors may be aligned on a line or a circular arc
- A modification of the algebraic reconstruction method is used to compute the image



Problem Extensions: Spiral CT

- A much more efficient way of acquiring a volume in CT
- Instead of acquiring a slice then shifting the table, the table moves continuously during the acquisition
- To compute a slice, interpolated projections are obtained from the 3D spiral then reconstructed as a regular 2D slice



Covered Material

- Parts of chapter 3 of Cierniak textbook
- Parts of chapter 15 of Hendee and Ritenour textbook