

Medical Equipment II - 2010

Magnetic Resonance Imaging⁽³⁾

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Web: <http://ymk.k-space.org/courses.htm>

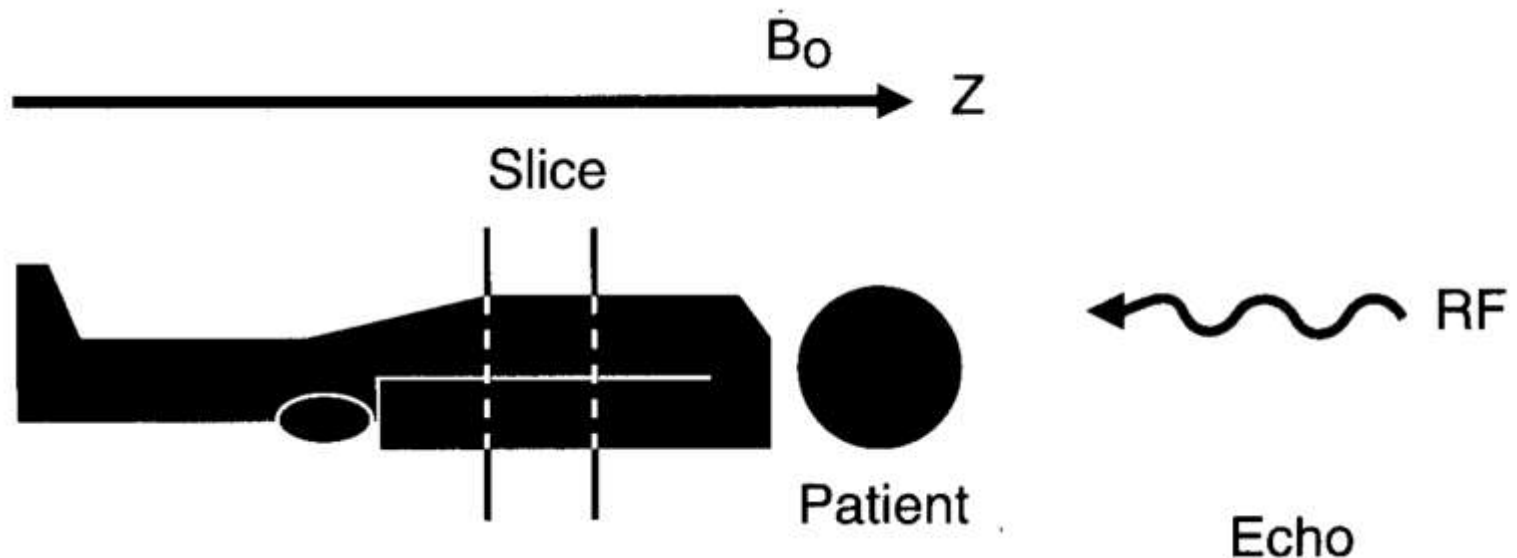


[Image Construction]

- Relies on **Spatial Encoding**
 - Differentiation between received signals from different locations
- In 3D, we need encoding in 3 orthogonal directions
 - **Slice selection**
 - **Frequency encoding**
 - **Phase encoding**
- Magnetic field gradients are key

[Slice Selection]

- Signal is obtained only from a particular slice from the body.
 - Can be in any direction



Slice Selection

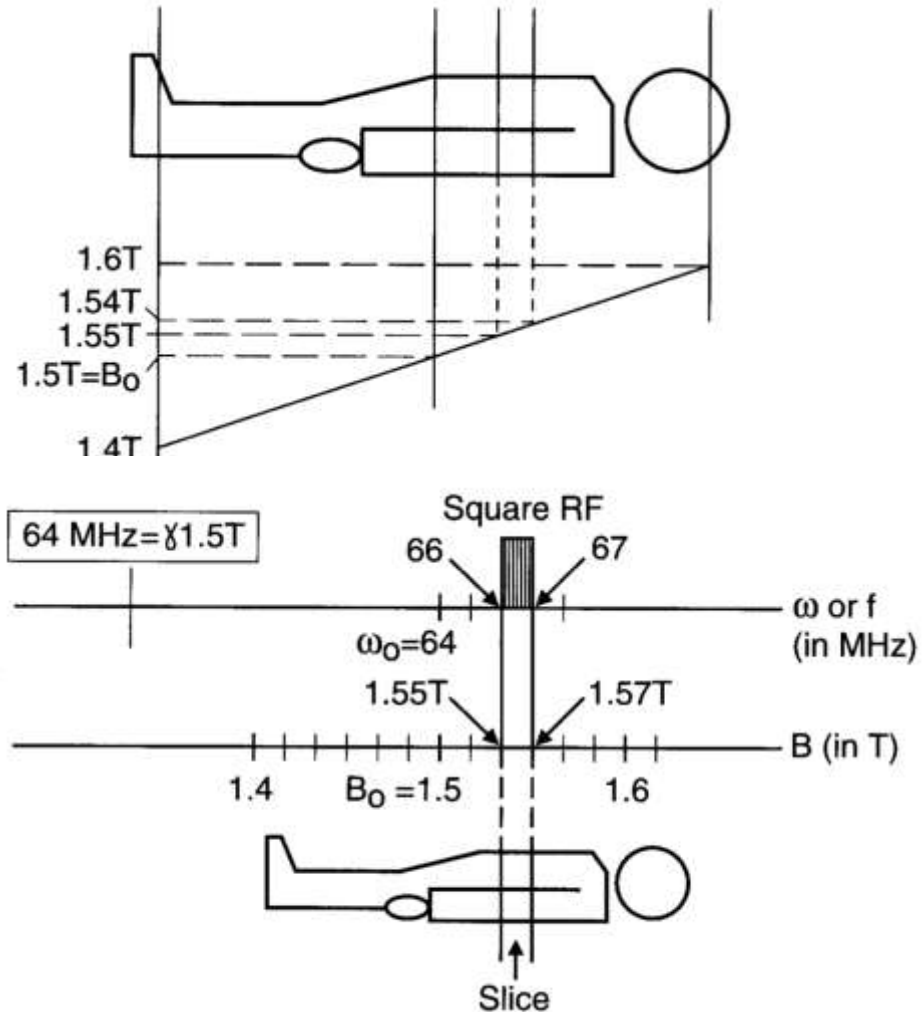
- Larmor equation:

$$\omega_o = \gamma B_0$$

- Larmor equation

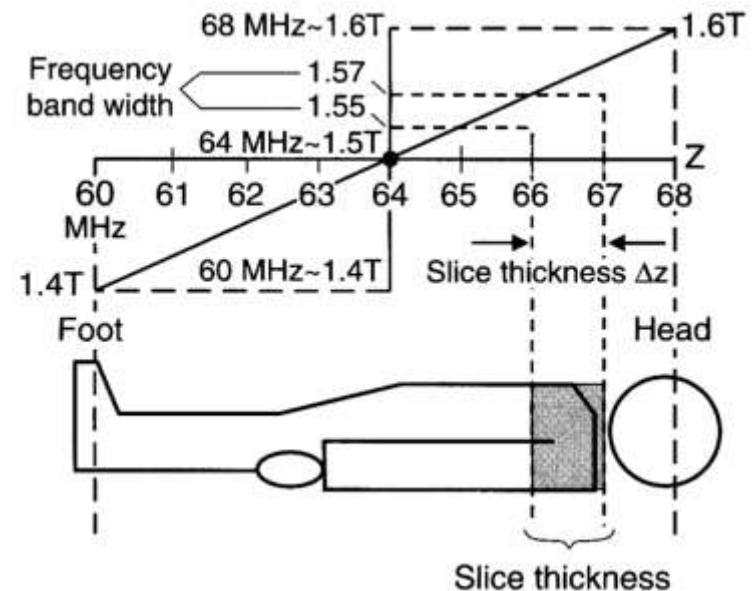
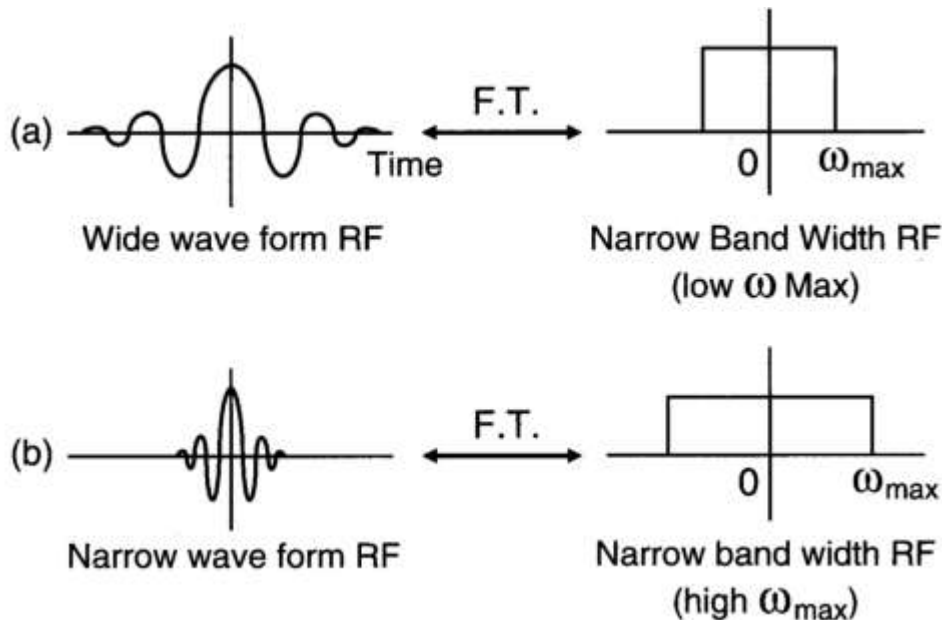
With z-gradient:

$$\omega_o(z) = \gamma(B_0 + G_z \cdot z)$$



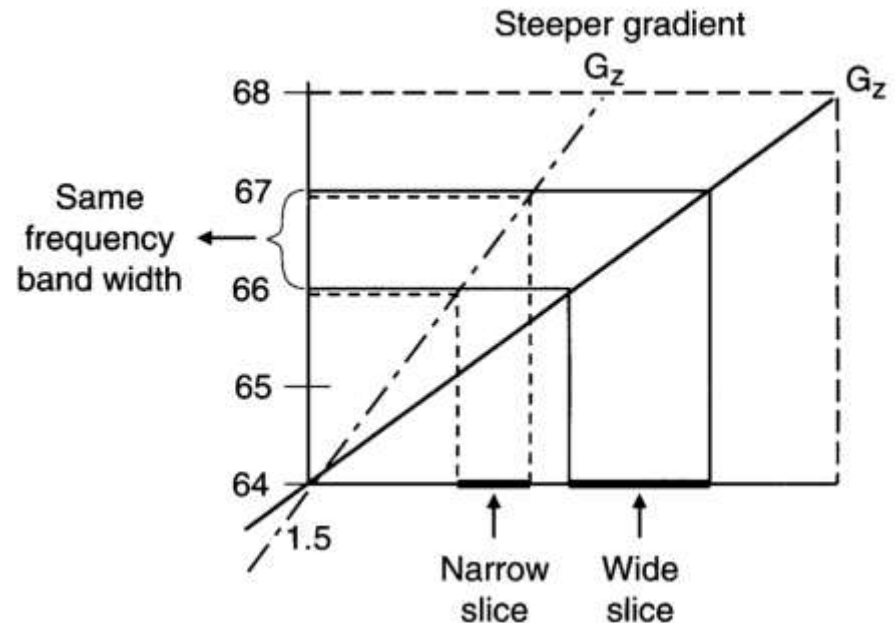
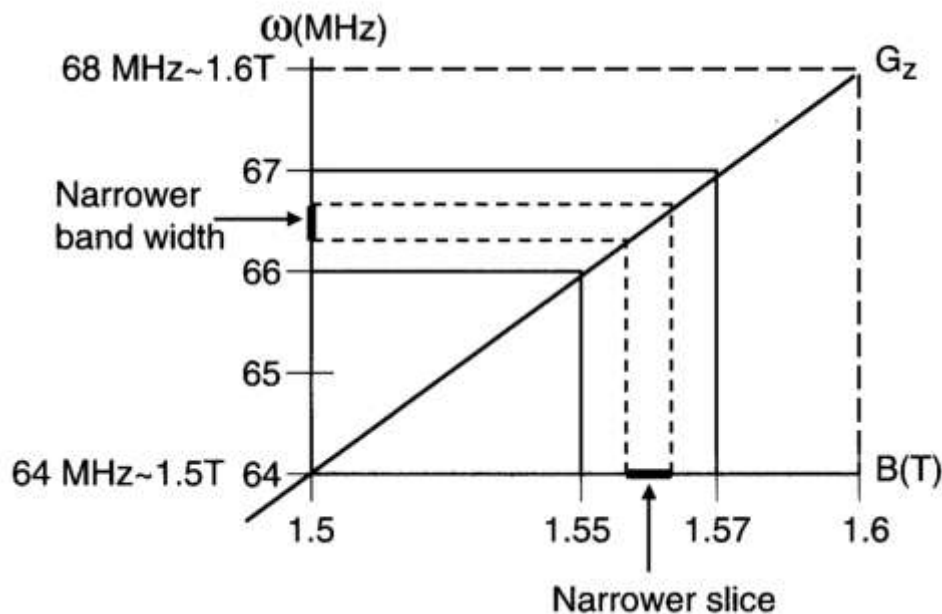
[Slice Selection]

- Slice parameters:
 - Slice position
 - Slice thickness



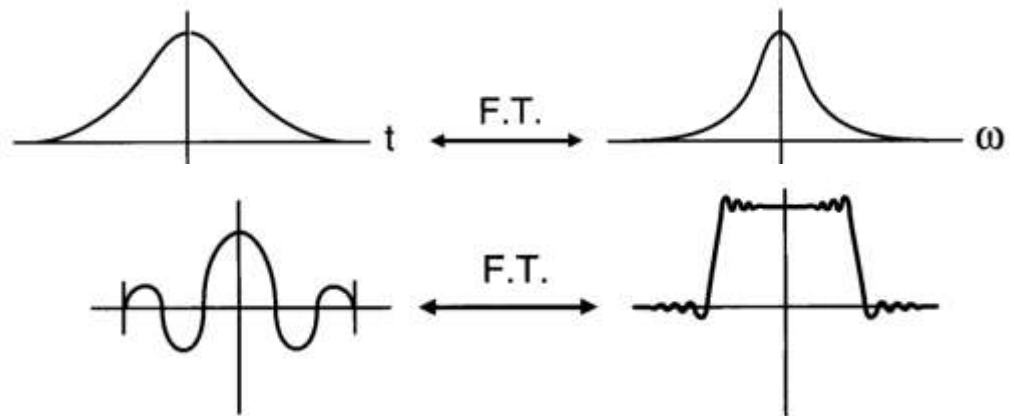
Slice Selection: Changing Slice Thickness

- Narrower RF pulse bandwidth
- Steeper slice selection gradient

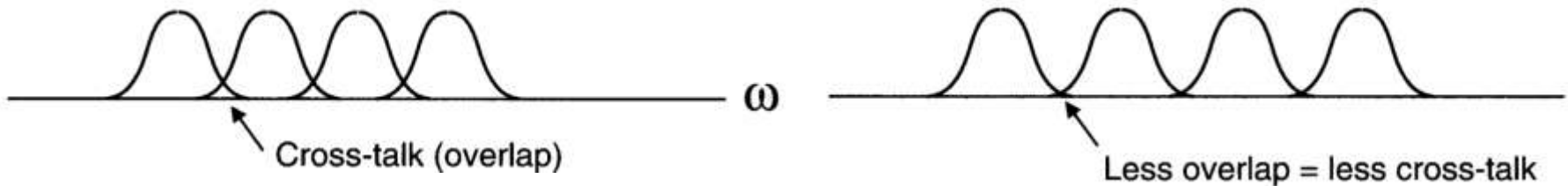


Slice Selection: Slice Profile and Crosstalk

- Slice profile = Fourier transform of pulse shape



- Cross-talk: overlap between slice profiles



[Fourier Encoding]

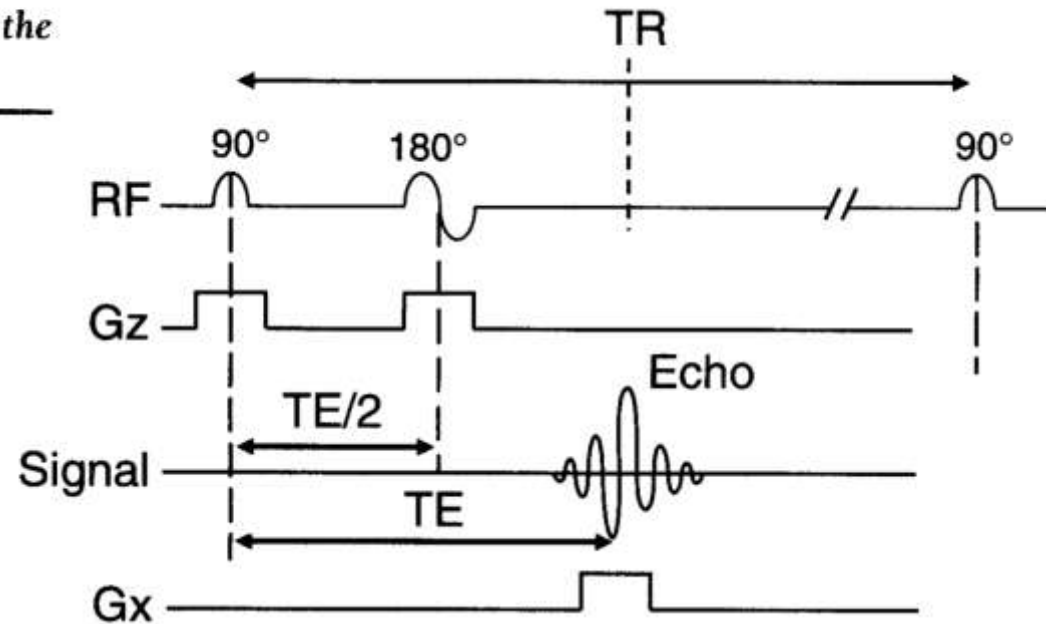
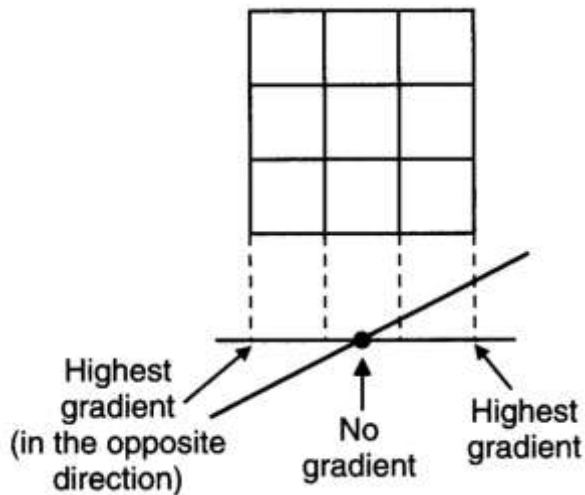
- Basic idea: encode location by frequency
 - Magnetic field gradient is used during reception
- Applied by 2 different methods
 - Frequency encoding
 - Phase encoding

[Frequency Encoding]

- Read-out gradient

$$F(k_x) = \int f(x) \cdot e^{-j2\pi k_x \cdot x} dx$$

The G_x gradient is applied during the time the echo is received, i.e., during read out.



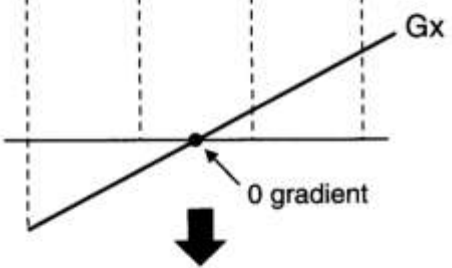
Frequency Encoding: Example

0	1	1
1	2	0
-2	0	1

With G_x
→

0	$\cos\omega t$	$\cos\omega t$
$\cos\omega t$	$2\cos\omega t$	0
$-2\cos\omega t$	0	$\cos\omega t$

No G_x
↓



0	$\cos\omega t$	$\cos\omega t$
$\cos\omega t$	$2\cos\omega t$	0
$-2\cos\omega t$	0	$\cos\omega t$

No encoding

→ $4 \cos\omega t$

0	$\cos\omega t$	$\cos\omega^+ t$
$\cos\omega^- t$	$2\cos\omega t$	0
$-2\cos\omega^- t$	0	$\cos\omega^+ t$

x-axis encoding

→ $(-\cos\omega^- t) + (3\cos\omega t) + (2\cos\omega^+ t)$

frequency ↔ position

Phase Encoding

- 2D Fourier transform

$$F(k_x, k_y) = \iint f(x, y) \cdot e^{-j2\pi(k_x \cdot x + k_y \cdot y)} dx dy$$

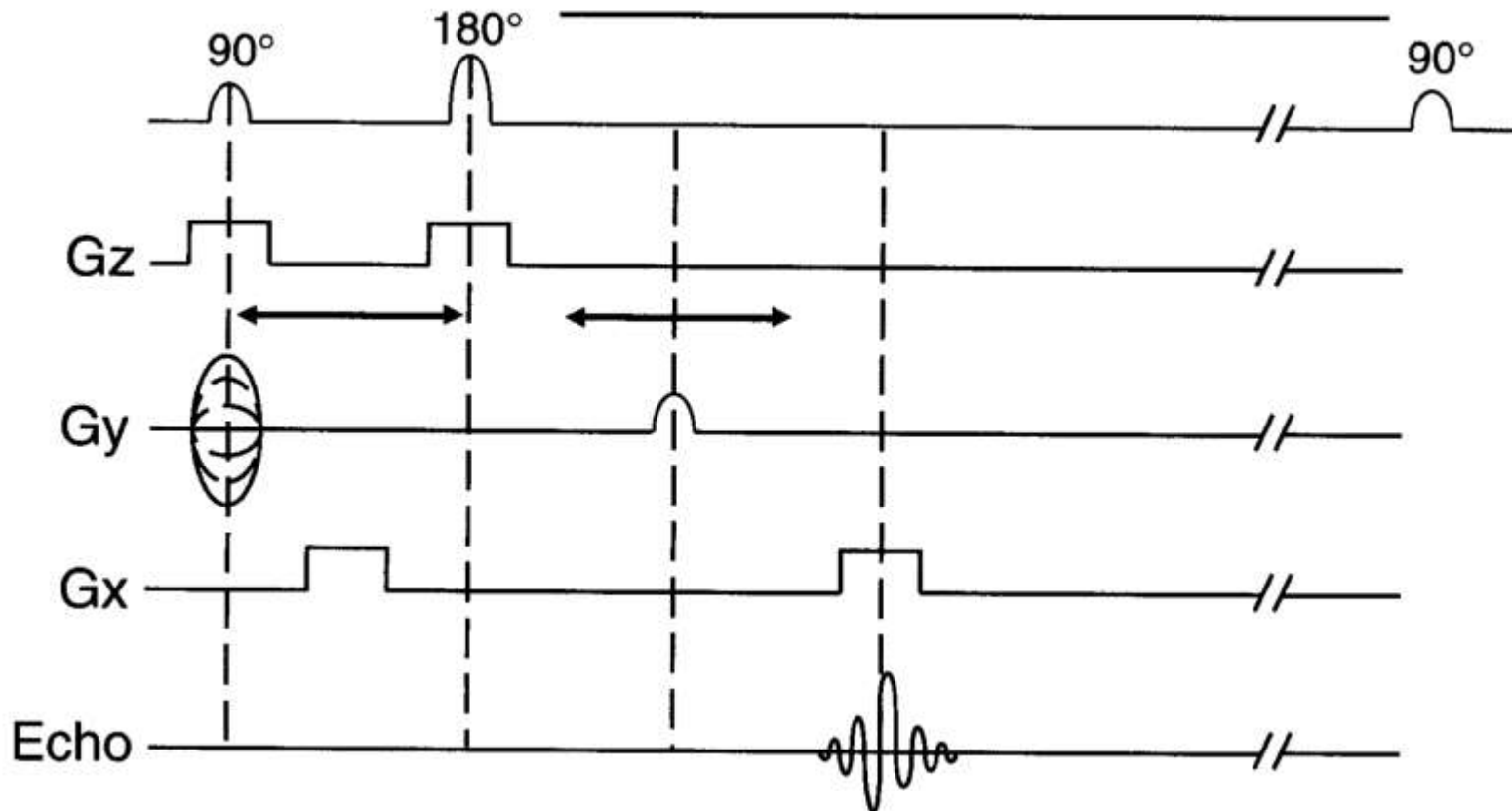
- With frequency encoding only:

$$F(k_x, 0) = \iint f(x, y) \cdot e^{-j2\pi(k_x \cdot x)} dx dy$$

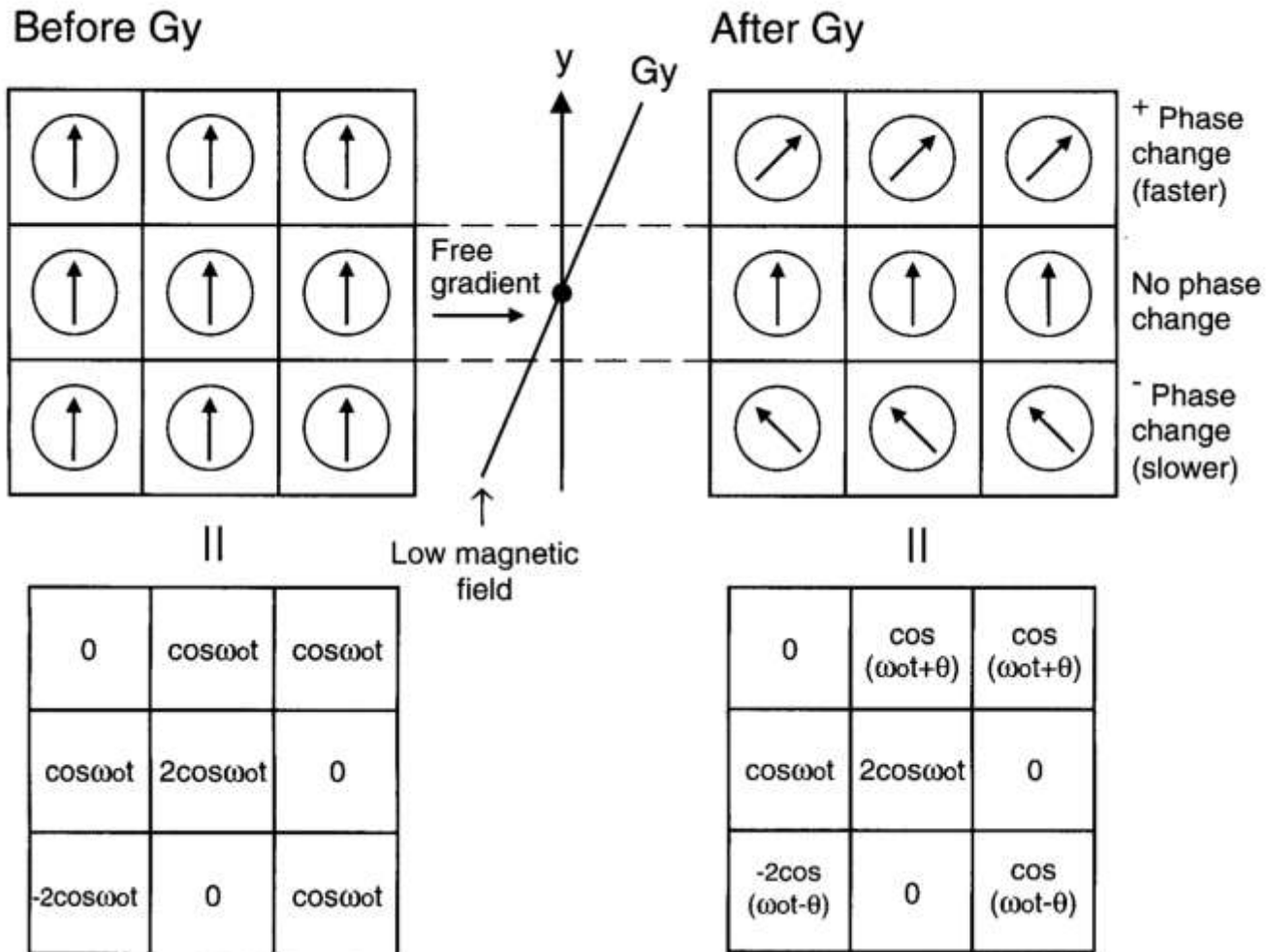
- Need to add another gradient in y-axis to encode spins in that direction

[Phase Encoding]

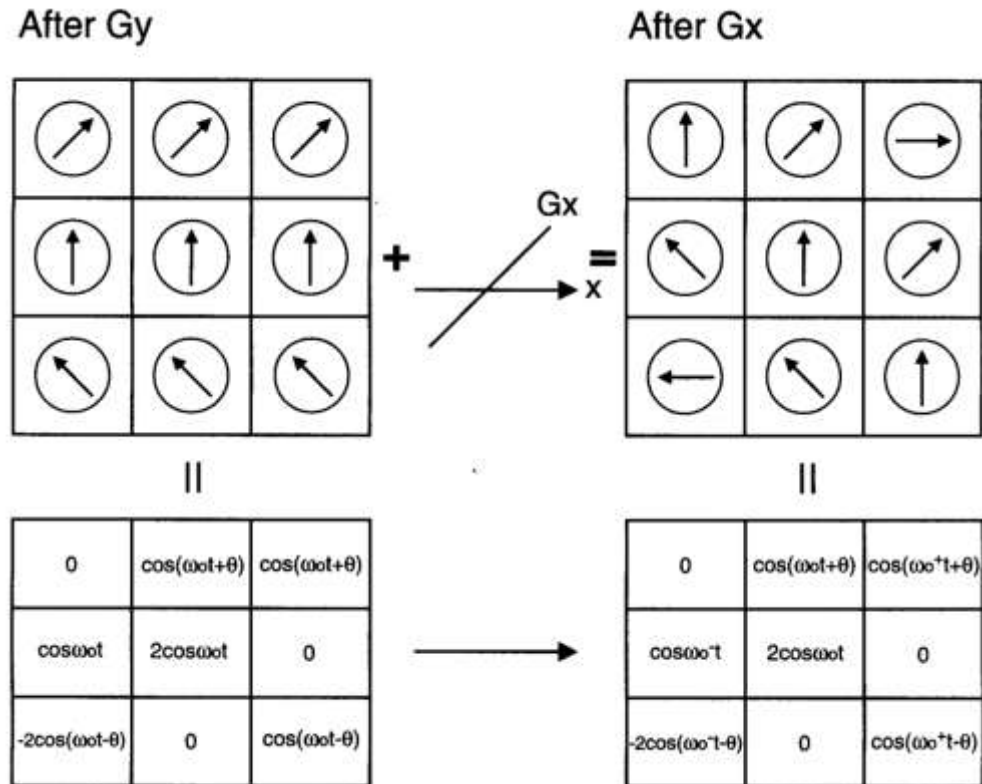
Gy is usually applied between the 90° and the 180° RF pulses or between the 180° pulse and the echo.



[Phase Encoding]



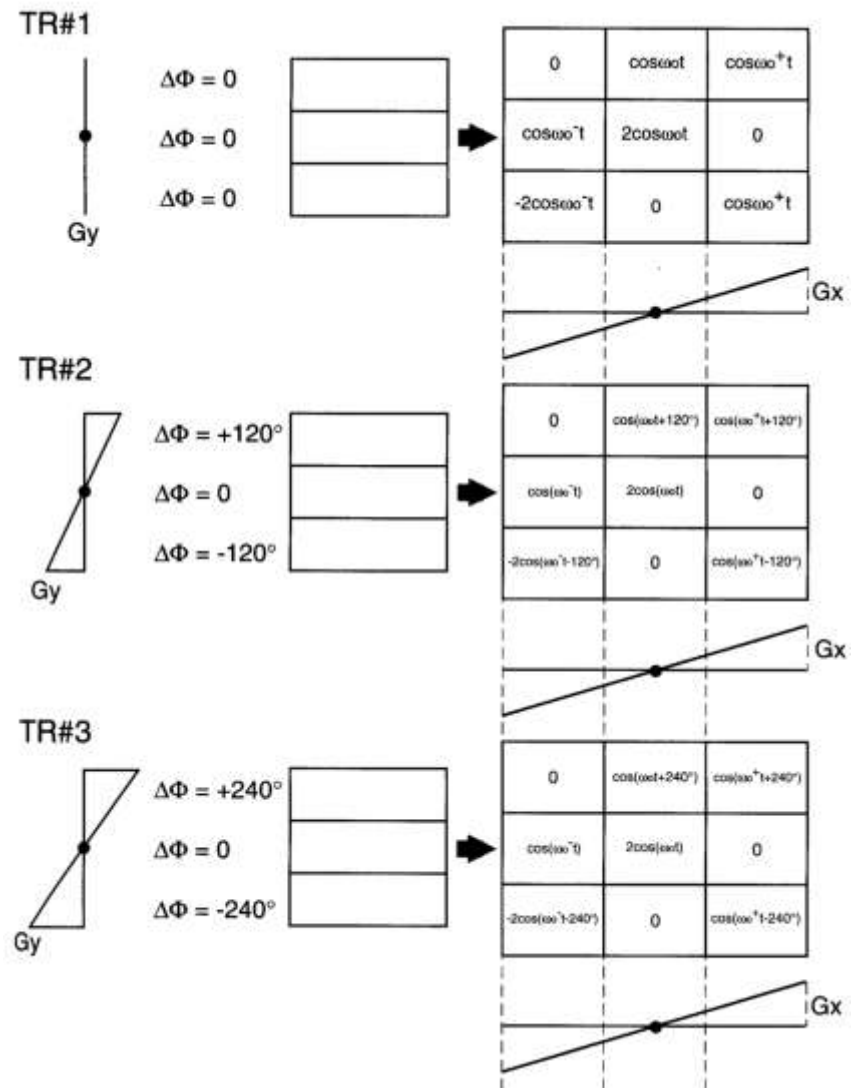
[Phase Encoding]



The protons in each pixel have a distinct frequency and a distinct phase, which are unique and encode for the x and y coordinates for that pixel.

[Phase Encoding]

- Each phase encoding requires 1 RF pulse
- Acquisition time = #phase encoding steps x TR



[Problem Assignments]

- Solve the problems at the end of each chapter.